Towards Anonymous Undercollateralized Loans

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Dong, Tim (University of Tennessee)

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• Asset-backed loans allow borrowers to pledge their assets as collateral for a loan

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- Asset-backed loans allow borrowers to pledge their assets as collateral for a loan
- Overcollateralization means collateral assets' value > loan value

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• Most DeFi loans are overcollateralized

• Credit lending is often considered impossible in DeFi due to its anonymity and permissionless nature (Harvey, Ramachandran, and Santoro, 2021)

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• Credit lending is often considered impossible in DeFi due to its anonymity and permissionless nature (Harvey, Ramachandran, and Santoro, 2021)

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• TrueFi is a platform that attempts to do credit lending.

- Credit lending is often considered impossible in DeFi due to its anonymity and permissionless nature (Harvey, Ramachandran, and Santoro, 2021)
- TrueFi is a platform that attempts to do credit lending.
- However, it operates exactly like a bank, with full KYB and allows only certain institutions.

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 \bullet All of DeFi loans are overcollateralized, with collateral-to-loan ratio ranging from 200% to 500%

- Credit lending is often considered impossible in DeFi due to its anonymity and permissionless nature (Harvey, Ramachandran, and Santoro, 2021)
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- \bullet All of DeFi loans are overcollateralized, with collateral-to-loan ratio ranging from 200% to 500%
- DeFi does not provide liquidity

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• Is it possible to have anonymous and permissionless undercollateralized lending? (whether it's on blockchain or not is irrelevant)

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• Financial privacy

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- Financial privacy
- Centralized credit info = More extreme consequences when data breaches occur

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- Financial privacy
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• Current financial system is not efficient and inclusive enough (Harvey, 2021)

- Financial privacy
- Centralized credit info = More extreme consequences when data breaches occur
- Current financial system is not efficient and inclusive enough (Harvey, 2021)
- DeFi can help, but it only offers overcollateralized lending

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• Early research regarding a semi-anonymous credit market was done by cryptographers

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- Early research regarding a semi-anonymous credit market was done by cryptographers
- Semi-anonymous because one party still know the identity of borrowers and may hold them accountable

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• Propose a model for anonymous (permissionless) and undercollateralized lending

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• Propose a model for anonymous (permissionless) and undercollateralized lending

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• Show conditions for incentive compatible loans

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• Credit history has value

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- Credit history has value
- Collaterals have opportunity cost

- Credit history has value
- Collaterals have opportunity cost
- Collateral loans are exposed to liquidation risk

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• Two types of players: borrower and a lending platform

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Players

- Two types of players: borrower and a lending platform
- A borrower has 3 possible strategies:
 - Never pay back credit loans (selfish)
 - Always pay back credit loans (honest)
 - Pay back only if collateral's value > principal + interests (mixed/strategic)

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- Two types of players: borrower and a lending platform
- A borrower has 3 possible strategies:
 - Never pay back credit loans (selfish)
 - Always pay back credit loans (honest)
 - Pay back only if collateral's value > principal + interests (mixed/strategic)
- A lending platform that:
 - Offers only overcollateralized lending to new users, i.e. users who have been borrowing for τ years
 - **②** After τ years, users can take under collateralized loans with no early liquidation

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• The user applies a discount rate *i* on every cash flow

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- The user applies a discount rate i on every cash flow
- $\bullet\,$ If the user hold onto his crypto, he/she can earn a yield of y

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- The user applies a discount rate i on every cash flow
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- Frictionless market

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- Returns are i.i.d

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- The user applies a discount rate i on every cash flow
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- Returns are i.i.d
- Overcollateralized loans are risk-free

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- Borrowers need to borrow P units of capital every period

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- Borrowers need to borrow P units of capital every period
- Borrowers can always pay back loans if want to

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- The user applies a discount rate i on every cash flow
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- Returns are i.i.d
- Overcollateralized loans are risk-free
- Borrowers need to borrow P units of capital every period
- Borrowers can always pay back loans if want to
- Asset prices are log-normal (*)
 - Only for convenience.

Table 1. Parameter definitions

Parameter	Meaning
P	loan amount
r	anonymous credit borrowing rate
au	number of periods (years) before credit loans are allowed
i	discount or risk-free rate
c	overcollateral borrowing rate
u	unobservable borrower's return from using the loan
y	return the borrower gains from holding his collateral assets
k	collateral-to-loan ratio for overcollateralized loans $(k > 1)$
l	collateral-to-loan ratio for undercollateralized loans $(l \leq 1)$
$ ho_t$	stochastic collateral assets' return
F	the probability $Pr(\rho_t < r)$

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• Gains from undercollateralized loans:

$$G \coloneqq (k-l)Py(1+\rho_H)$$

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• Gains from undercollateralized loans:

$$G \coloneqq (k-l)Py(1+\rho_H)$$

• If pay back on undercollateralized loans:

$$H \coloneqq P(u - r + l\rho_H) + G$$

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• Gains from undercollateralized loans:

$$G \coloneqq (k-l)Py(1+\rho_H)$$

• If pay back on undercollateralized loans:

$$H \coloneqq P(u - r + l\rho_H) + G$$

• If default on undercollateralized loans:

$$S \coloneqq P(u+1-l) + G$$

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• Gains from undercollateralized loans:

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• If pay back on undercollateralized loans:

$$H \coloneqq P(u - r + l\rho_H) + G$$

• If default on undercollateralized loans:

$$S \coloneqq P(u+1-l) + G$$

• For overcollateralized loans:

$$B \coloneqq P(u-c)$$

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Visualization of payoffs for $\tau = 2$



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• For overcollateralized loans, all strategies give the same payoffs

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• For overcollateralized loans, all strategies give the same payoffs

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• The only time when strategies matter is for credit/undercollateralized loans

- For overcollateralized loans, all strategies give the same payoffs
- The only time when strategies matter is for credit/undercollateralized loans
- Only need to compute the expected payoff differences up to the point of options, i.e., where the borrowers can choose.

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Visualization of payoffs for $\tau = 2$



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Main result

 $\mathbb{E}[H(r) - M(r)] > 0$

$$\Leftrightarrow \frac{F(D_{HB}e^{(-2\tau-1)i}(1-F)^{\tau+1})}{(e^{i}-1+F)(e^{i}-1)} + \frac{F\left((-D_{HB}+D_{HS})e^{-i(\tau+1)}-D_{HS}e^{-i\tau}\right)(1-F)^{\tau+1}}{(e^{i}-1+F)(e^{i}-1)} + \frac{F(D_{HS}e^{i}+D_{HB}-D_{HS}e^{-i\tau}D_{HB})}{(e^{i}-1+F)(e^{i}-1)} > 0$$
(1)

where

$$\begin{aligned} \mathbf{D}_{HS} &= \mathbb{E}\left[H_B - S_B \mid l(1+\rho_t) < 1+r\right] \\ &= \mathbb{E}\left[P(l(1+\rho_t) - (1+r)) \mid l(1+\rho_t) < 1+r\right] < 0 \\ \mathbf{D}_{HB} &= \mathbb{E}\left[H_B - B_B\right] \\ &= P\left(c - r + l\bar{\rho}\right) + (k-l) Py\left(1+\bar{\rho}\right) \end{aligned}$$

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• It might be possible to have incentive compatible anonymous credit lending market

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- It might be possible to have incentive compatible anonymous credit lending market
- Honest incentive compatible credit rate does not depend on borrower's return

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- It might be possible to have incentive compatible anonymous credit lending market
- Honest incentive compatible credit rate does not depend on borrower's return
- Higher τ leads to higher honest advantage, but at a diminishing rate

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- It might be possible to have incentive compatible anonymous credit lending market
- Honest incentive compatible credit rate does not depend on borrower's return
- Higher τ leads to higher honest advantage, but at a diminishing rate
- Higher collateral asset's expected return linearly and positively correlate with higher credit rate

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- Utilize cadCAD framework
 - cadCAD has been applied in production, e.g. THORChain

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- Utilize cadCAD framework
 - cadCAD has been applied in production, e.g. THORChain
- Validate theoretical results and extend to more complex scenarios

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• Borrowers may invest differently conditional on the type of loans

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- Borrowers may invest differently conditional on the type of loans
- $\bullet\,$ Moral hazard causes the unobserved borrower return, u, to appear in the profit difference

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- Borrowers may invest differently conditional on the type of loans
- Moral hazard causes the unobserved borrower return, u, to appear in the profit difference

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• If the expected utility maximization assumption holds, then the results are unchanged. See Figure 3

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Validating theoretical results



Figure: Formula validation (SPY as the underlying asset)

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Comparative statics



Figure: Comparative statics

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Moral hazard



Figure: Moral hazard

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Accidental default



Figure: Accidental default

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• I show the conditions for an incentive-compatible anonymous undercollateralized loan market

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- I show the conditions for an incentive-compatible anonymous undercollateralized loan market
- The results provide the theoretical foundation for P2P undercollateralized loan market and can help scale up this type of market

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