

A Portfolio Model of Quantitative Easing

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- Consensus that QE reduced long-term interest rates
- But the transmission to long rates is not well understood, conceptually and empirically
- Notably, lack of theoretical accounting for role of central bank reserves and commercial banks
- Transmission details matter for how to best design, calibrate, communicate, and exit QE programs

- We present a portfolio model with a CB, reserve-holding banks, and non-bank financial institutions
- Two financial frictions, imperfect substitutability and segmentation of the market for central bank reserves, lead to two distinct portfolio balance effects:
 - Standard supply induced effects due to a lower available supply of the purchased assets, and
 - Reserve induced portfolio effects, independent of the specific assets purchased
- Application: Impact of leverage constraints on QE transmission

- 1 Non-technical Overview
- 2 The Model
- 3 Empirical Relevance
- 4 Conclusions and Implications

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Existing PB Models Missing Important Aspects of QE

- Previous PB models of QE one-sided:
 - Seminal paper: Vayanos Vila 2009
 - No role for reserves or banks
 - CB bond purchases modelled as exogenous reduction in supply
 - Price re-equilibrates demand and supply





- What about the other side of the QE transaction? CB reserves
 - Bernanke and Reinhart (2004) argue that an expansion of reserves by itself can have PB effects
 - ...but do not present a model of the mechanism.



We Include Reserves and Banks in a PB Model



Portfolio model of a financial market:

- Three actors: CB, banks and non-bank financial firms
- Four assets: long bonds, short bonds, bank deposits and central bank reserves
- Two central frictions (more can be added):
 - Only banks can hold reserves, and
 - Imperfect asset substitutability
- Central assumption:
 - Banks' bond demand propensity out of new funding is positive, given asset prices

Intuition for Reserve-Induced Effects (1)

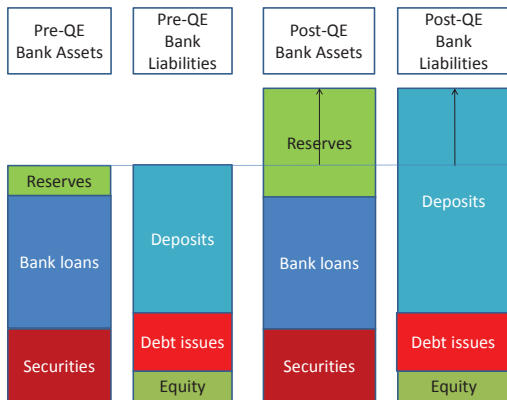
Banks	
<u>Assets</u>	<u>Liabilities</u>
Reserves  	Equity
Short bonds 	Deposits 
Long bonds	Other debt
Other assets	

Central Bank	
<u>Assets</u>	<u>Liabilities</u>
Short bonds 	Equity
Long bonds	Reserves 
Other assets	Other liabilities

Non-Bank Financial Firms	
<u>Assets</u>	<u>Liabilities</u>
Deposits 	Equity
Short bonds 	Debt
Long Bonds	
Other assets	

- Example: CB purchases short bonds from banks (green)
- Standard macro: short bonds and money perfect substitutes at ZLB, no effect
- Now consider purchases from non-banks (black arrows)

Intuition for Reserve-Induced Effects (2)



- Initial impact: Bank balance sheets extend, their demand for non-reserve assets increases
- The extra reserves must stay in banks: Hot potato effect....
- ... until longer-duration yields decline enough to make banks content to hold the extra reserves

Intuition for Reserve-Induced Effects (3)

Banks	
<u>Assets</u>	<u>Liabilities</u>
Reserves ↑	Equity
Short bonds ↑	Deposits ↑
Long bonds ↓	Other debt
Other assets	

Central Bank	
<u>Assets</u>	<u>Liabilities</u>
Short bonds	Equity
Long bonds ↑	Reserves ↑
Other assets	Other liabilities

Non-Bank Financial Firms	
<u>Assets</u>	<u>Liabilities</u>
Deposits ↑	Equity
Short bonds	Debt
Long Bonds ↓	
Other assets	

- Reserve-induced effects arise when assets are purchased from non-banks, and are independent of the assets
- Long bonds can have both reserve and supply effects

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Modelling Approach and Versions

- One period model of asset market equilibrium with smallest number of features to illustrate that reserves matter
- Long-term bond demand assumptions:
 - Imperfect substitutability: $-\infty < \frac{\partial f_i}{\partial P_L} < 0$
 - Banks' bond demand propensity out of new funding:
 $0 < \frac{\partial f_B}{\partial D'_B} < 1$
- Different model versions:
 - Benchmark model with one traded security (the long bond, L): simple, tractable, captures all effects
 - Two traded securities version (long and short bonds): confirms findings of one-security version

Solution in One-Security Model Version

- The equilibrium bond price ensures aggregate demand for bonds in banks and non-banks equals total supply of bonds net of central bank holdings
- Comparative statics. Change in equilibrium bond price associated with a QE transaction:

$$\frac{dP_L}{dL_{CB}} = \frac{-1}{\frac{\partial f_{NB}}{\partial P_L} + \frac{\partial f_B}{\partial P_L} - P_L \frac{\partial f_{NB}}{\partial P_L} \frac{\partial f_B}{\partial D_B}}$$

- First two terms in denominator are supply induced effects. Third term is reserve induced effect
- Price impact depends on price sensitivity of bond demand, and banks' bond demand propensity from new funding

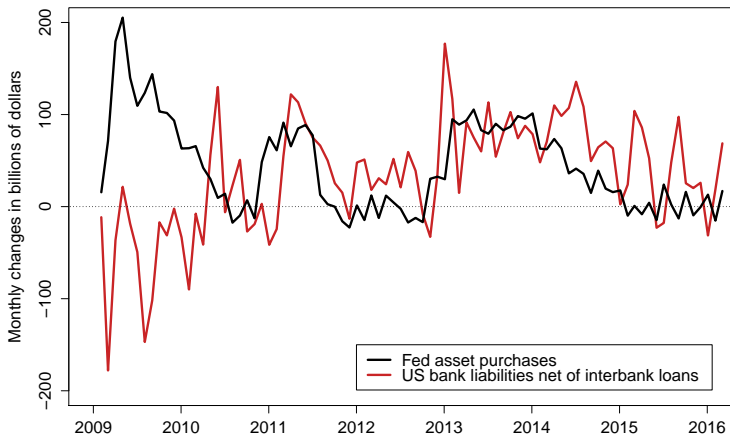
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Are Reserve-Induced Effects Empirically Relevant?

- To identify reserve effects, we need QE-style CB reserve expansions without long-term bond purchases
- The Swiss reserve expansion program of August 2011:
 - Akin to natural experiment of QE in short-term bonds
 - Christensen and Krogstrup (FRBSF WP 2016) find support for reserve induced effects
- Event studies of US and UK QE cannot identify, but:
 - Exit may provide insights: Bonds roll off - reserves effect?
 - Studies indicate non-bank counterparties and bank balance sheet expansions associated with parts of QE (Joyce et al. 2011, Ennis and Wollman 2015, Carpenter et al. 2013)

Empirical Relevance of Reserve-Induced Effects

- Data on bank total liabilities suggest the conditions were there for reserve induced effects during QE2 and QE3:



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We develop a portfolio model of QE transmission to asset prices that includes central bank reserves and banks

- **Main finding:** PB effects come in two variants
 - Supply induced PB effect
 - Reserve induced PB effects
- **The distinction matters.** Reserve effects are different:
 - Independent of the assets that central bank is purchasing
 - Depend on features of market and banking system (preferences and constraints)
- **Empirically relevant.** Effects shown for Swiss reserve expansions. Likely to have played a role BoE and Fed QE

Implications for the design and transmission of QE programs:

- **Which assets to buy?** Not necessary to buy long-dated securities to affect long-term yields
- **Financial institutional structure matters.** Who has access to reserves, and preferred habitat investors
- **Role of bank regulation** in transmission: bank leverage constraints and portfolio risk management models of non-banks matter
- **Transmission and Exit:** Rolling off of bonds akin to sales of short bonds. Reverse reserve effects?

Thank you!

Model With One Traded Security

One period model of asset market equilibrium

- Three types of actors:
 - A central bank (*CB*)
 - An infinity of reserve holding commercial banks (*B*)
 - An infinity of non-bank financial firms (*NB*)
- Three types of assets (simplest case):
 - Long bonds, L , with the price of P_L and $TP = 1 - P_L$
 - Central bank reserves, R , with the price of one (numeraire)
 - Bank deposits, D with the price of one

The Model (2)

The central bank balance sheet:

- $P_L L_{CB} = E_{CB} + R$
 - L_{CB} : is the central bank's holdings L
 - E_{CB} is the value of the central bank's initial equity
 - R is outstanding reserves

Policy tool is bond purchases, $P_L dL_{CB}$, paid for by reserves, dR , and equity is residually determined by bond price changes:

- $dE_{CB} = dP_L L_{CB} + P_L dL_{CB} - dR$

The Model (3)

The non-bank financial firm j balance sheet:

- $P_L L_{NB}^j + D_{NB}^j = E_{NB}^j$
 - L_{NB}^j is firm j 's holdings of bonds
 - D_{NB}^j holdings of bank deposits
 - E_{NB}^j initial equity value

Non-banks obtain deposits by selling bonds and vice versa, equity is residually determined by price changes:

- $dE_{NB}^j = dP_L L_{NB}^j + P_L dL_{NB}^j + dD_{NB}^j$

The Model (4)

Non-bank financial firms balance their liquid portfolio between deposits and bonds, demanding positive amounts of both:

- $L_{NB}^j = f_{NB}(P_L, E_{NB}^j)$
- $\frac{\partial f_{NB}}{\partial P_L} < 0$ Normal downward sloping demand Substitutability
- $\frac{\partial f_{NB}}{\partial E_{NB}} = 0$ No real-time reaction to changes in equity value.
Allows more tractability, not central for results

The demand for deposits is determined as a residual:

- $D_{NB}^j = E_{NB}^j - P_L f_{NB}(P_L, E_{NB}^j)$

The Model (5)

Depository bank i balance sheet:

- $R^i + P_L L_B^i = E_B^i + D_B^i$
 - L_B^i is bank i 's holdings of bonds
 - R^i is its holdings of central bank reserves
 - D_B^i is the bank's deposit funding
 - E_B^i initial equity value

Banks can obtain reserves by selling bonds. Reserves fluctuate autonomously when bank costumers trade bonds for deposits:

- $dR^i = dD_B^i - P_L dL_B^i$

Bank equity is residually determined by bond-price changes:

- $dE_B^i = dP_L L_B^i$

The Model (6)

Depository banks' demand for bonds and reserves:

- $L_B^i = f_B(P_L, E_B^i + D_B^i)$

Central assumptions:

- $\frac{\partial f_B}{\partial P_L} < 0$ Normal good, imperfect substitutability
- $0 < \frac{\partial f_B}{\partial D_B^i} < 1$ Bank "maturity transformation" assumption

The demand for reserves is determined as a residual:

- $R_B^i = E_B^i + D_B^i - P_L f_B(P_L, E_B^i + D_B^i)$

- Assume no market power of individual financial institutions:
Continuum of identical banks and nonbanks, normalized to 1:
Drop equation subscripts
- The equilibrium bond price ensures aggregate demand for bonds in banks and non-banks equals total supply of bonds net of central bank holdings
- Comparative statics: We analyze the change in equilibrium bond price associated with a QE transaction:
- $-dL_{CB} = dL_B + dL_{NB}$