

Survival ambiguity and welfare

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AEA Philadelphia Jan 2018

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- Why? Many of the factors that determine survival probabilities are unobservable.
- ...but the family of distributions from which one's survival probabilities are drawn is known.

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- 4 Evaluate the role of public insurance (Social Security):
 - SS does not help to hedge survival ambiguity.

Measurement of ambiguity

Structural calibration

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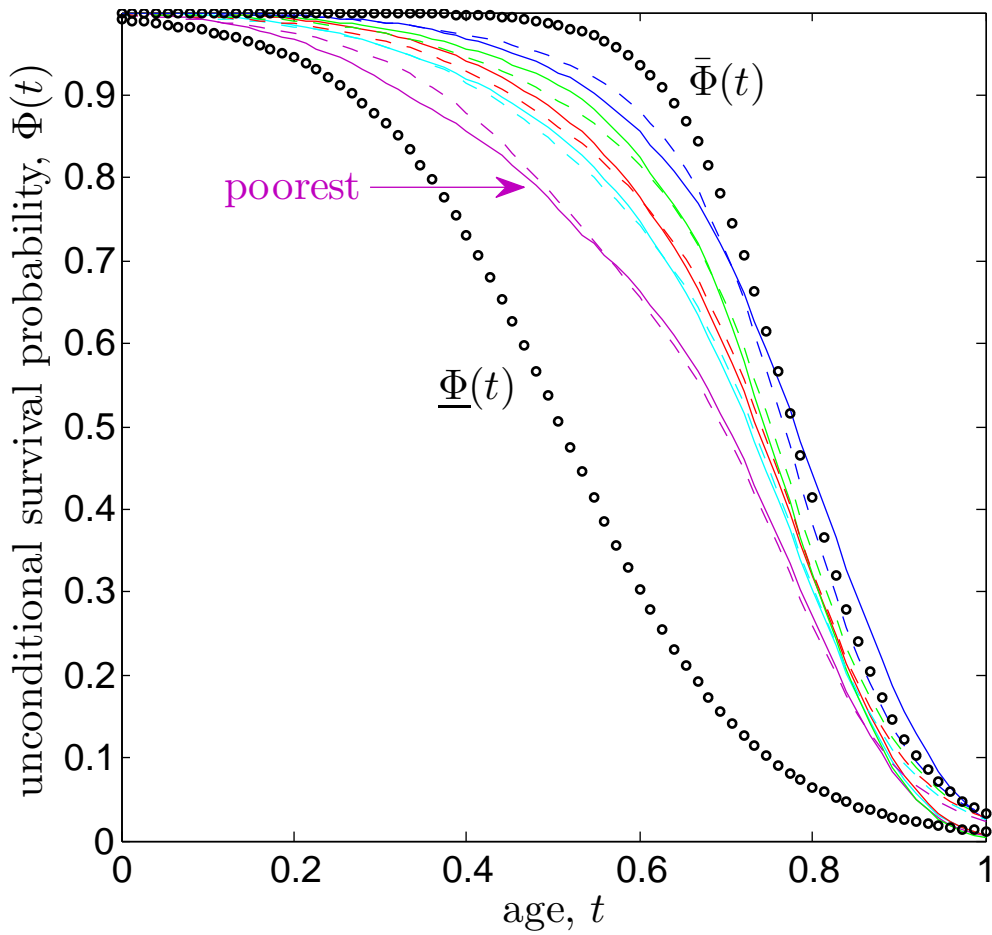
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- At $t = 0$, p_i is the subjective (prior) probability of being a low type for an individual in quintile i . Expected utility maximizers make plans with a convex combination $p_i \underline{\Phi}(t) + (1 - p_i) \bar{\Phi}(t)$.

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- Given the actual survival data by quintile $\Phi_i(t)$, our calibration problem:

$$\min_{\underline{\Phi}(t), \bar{\Phi}(t), p_i} \mathcal{L} = \sqrt{\sum_{i=1}^5 \int_0^1 \{\Phi_i(t) - [p_i \underline{\Phi}(t) + (1 - p_i) \bar{\Phi}(t)]\}^2 dt}$$

Figure 1. Calibration of Mortality and Binary Ambiguity by Income Quintile



Note: Solid lines are data. Dashes and circles are calibrated.

Welfare cost of ambiguity

Theory

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- Define three objective functionals

$$J^* = \int_0^1 [p\underline{\Phi}(t) + (1-p)\bar{\Phi}(t)]u(c(t))dt$$

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- and three optimal consumption paths

$$c^*(t) = \arg \max J^*$$

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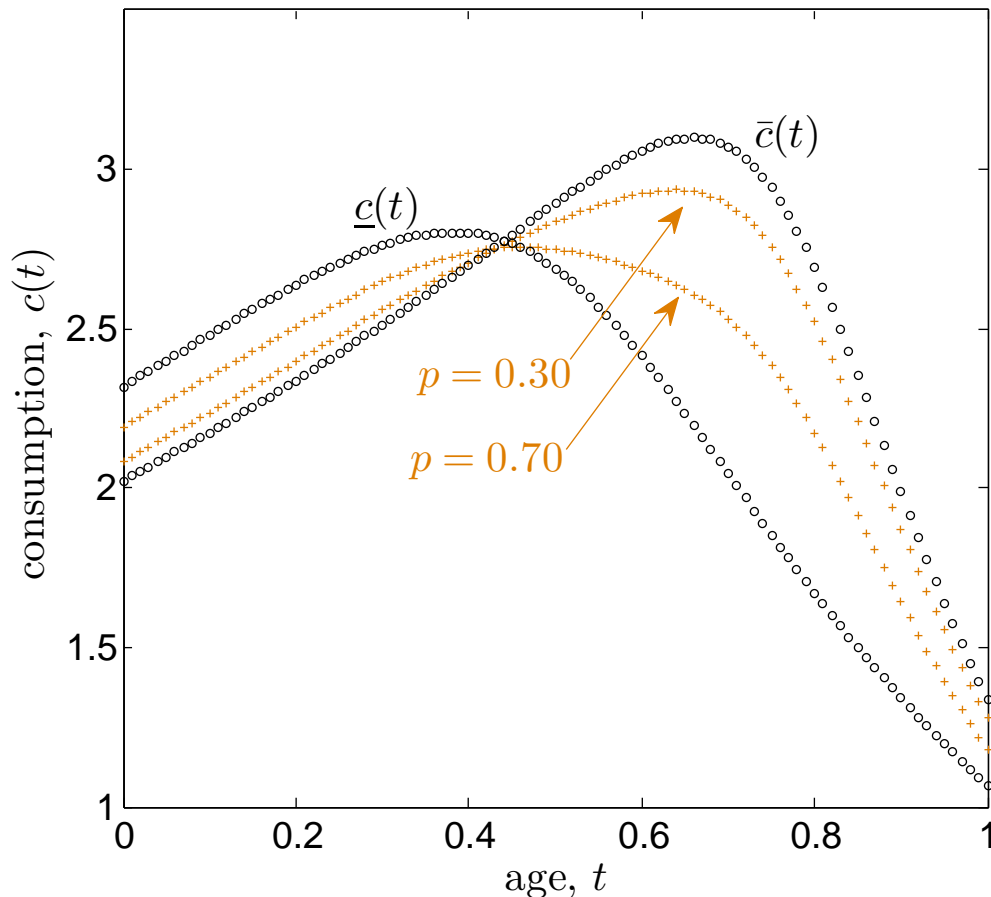
- Ambiguity is costly because decisions are distorted away from their full information counterparts where the individual fully optimizes based on known survival risk.

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- Survival ambiguity is **highly regressive**: cost to the poorest quintile is 4 times larger than the cost to the richest quintile.
- Why? The poor rationally believe there is a strong chance they are a low survival type, causing them to save very little relative to what they would save if they knew they were a high type: ambiguity causes a painful “undersaving” problem among the poor who are the high survival type.

Figure 4. Fair Comparison of Consumption under Binary Ambiguity



Note: Plus marks are consumption under ambiguity. Circles are consumption when the survival type is known in advance.

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 - Brown, Kapteyn, Luttmer, and Mitchell (2016) quantify the degree to which individuals are cognitively constrained in their internal valuation of annuities.

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- 1 Only two survival types.
 - With a continuum of survival types, the magnitude of the welfare cost goes down but the regressivity result persists.
- 2 Individuals form priors about survival type based solely on their position in the income distribution.
 - While survival risk is strongly connected to income class (e.g., Cristia (2009)), other non-income factors could be informative about survival type.

Private insurance (annuities)

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- Individuals save for retirement with competitive annuity contracts as in Yaari (1965) but expanded to incorporate ambiguity.
- Insurance companies cannot separate people by survival type because that information is unknown.
- Instead, they pool everyone together and offer a zero-profit contract with competitive return

$$r(t) = -\frac{\frac{d}{dt}[p\underline{\Phi}(t) + (1-p)\bar{\Phi}(t)]}{p\underline{\Phi}(t) + (1-p)\bar{\Phi}(t)}.$$

- In contrast, without ambiguity, insurance companies have full information about survival type and offer separate competitive contracts to each type

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- Ambiguity distorts c away from what the individual would do with full information about survival risk (which is bad).
- *But* ambiguity also causes competitive insurance companies to pool risk across survival type.

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- These two results combine to create a final result: welfare gains from competitive annuities are larger with ambiguity than without ambiguity.
- Past studies underestimate the welfare gains from annuitization because they abstract from survival ambiguity.
- Competitive annuities not only insure *survival risk* as past studies have established, but they also pool risk across *survival type*.

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- Hence, while asymmetric information about survival risk can rationalize thin annuity markets, ambiguity about survival risk makes thin annuity markets even more puzzling.

Social Security

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- While SS can improve welfare by providing a life annuity, the cost of survival ambiguity is the same whether SS exists or not (SS does not affect willingness to pay for immediate resolution of ambiguity).
- Likewise, the welfare gain from SS's provision of a life annuity is the same with or without ambiguity.

Thank you

