

Measuring the Bias of Technological Change*

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Abstract

Technological change can increase the productivity of the various factors of production in equal terms or it can be biased towards a specific factor. We directly assess the bias of technological change by measuring, at the level of the individual firm, how much of it is labor augmenting and how much is factor neutral. To do so, we develop a framework for estimating production functions when productivity is multi-dimensional. Using panel data from Spain, we find that technological change is biased, with both its labor-augmenting and its factor-neutral component causing output to grow by about 2% per year.

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1 Introduction

When technological change occurs, it can increase the productivity of capital, labor, and the other factors of production in equal terms or it can be biased towards a specific factor. Whether technological change favors some factors of production over others is central to economics. Yet, the empirical evidence is relatively sparse.

The literature on economic growth rests on the assumption that technological change increases the productivity of labor vis-à-vis the other factors of production. It is well known that for a neoclassical growth model to exhibit steady-state growth either the production function must be Cobb-Douglas or technological change must be labor augmenting (Uzawa 1961), and many endogenous growth models point to human capital accumulation as a source of productivity increases (Lucas 1988, Romer 1990). A number of recent papers provide microfoundations for the literature on economic growth by theoretically establishing that profit-maximizing incentives can ensure that technological change is, at least in the long run, purely labor augmenting (Acemoglu 2003, Jones 2005). Whether this is indeed the case is, however, an empirical question that remains to be answered.

One reason for the scarcity of empirical assessments of the bias of technological change may be a lack of suitable data. Following early work by Brown & de Cani (1963) and David & van de Klundert (1965), economists have estimated aggregate production or cost functions that proxy for labor-augmenting technological change with a time trend (Lucas 1969, Kalt 1978, Antràs 2004, Klump, McAdam & Willman 2007, Binswanger 1974, Jin & Jorgenson 2010).¹ This line of research has produced some evidence of labor-augmenting technological change. However, the intricacies of constructing data series from national income and product accounts (Gordon 1990, Krueger 1999) and the staggering amount of heterogeneity across firms in combination with simultaneously occurring entry and exit (Dunne, Roberts & Samuelson 1988, Davis & Haltiwanger 1992) may make it difficult to interpret a time trend as a meaningful average economy- or sector-wide measure of technological change. Furthermore, this line of research does not provide any deeper insights into the anatomy of the underlying productivity distribution. It also pays scant attention to the fundamental endogeneity problem in production function estimation. This problem arises because a firm's decisions depend on its productivity, and productivity is not observed by the econometrician, and it may severely bias the estimates (Marschak & Andrews 1944).²

While traditionally using more disaggregated data, the productivity and industrial organization literatures assume that technological change is factor neutral. Hicks-neutral

¹A much larger literature has estimated the elasticity of substitution using either aggregated or disaggregated data whilst maintaining the assumption of factor-neutral technological change, see Hammermesh (1993) for a survey.

²Intuitively, if the firm adjusts to a change in its productivity by expanding or contracting its production, then unobserved productivity and input usage are correlated, resulting in biased estimates of the production function. See Griliches & Mairesse (1998) and Akerberg, Benkard, Berry & Pakes (2007) for reviews of this and other problems involved in the estimation of production functions.

technological change underlies, either explicitly or implicitly, most of the standard techniques for measuring productivity, ranging from the classic growth decompositions of Solow (1957) and Hall (1988) to the recent structural estimators for production functions that resolves the endogeneity problem (Olley & Pakes 1996, Levinsohn & Petrin 2003, Akerberg, Caves & Frazer 2006, Doraszelski & Jaumandreu 2013, Gandhi, Navarro & Rivers 2013). In their present form these techniques therefore do not allow us to assess whether technological change is biased towards some factors of production.

In this paper, we combine firm-level panel data that is now widely available with advances in econometric techniques to directly assess the bias of technological change by measuring, at the level of the individual firm, how much of technological change is labor augmenting and how much of it is Hicks neutral. To do so, we develop a framework for estimating production functions when productivity is multi-dimensional and has a labor-augmenting and a Hicks-neutral component.

Our framework accounts for firm-level heterogeneity in the components of productivity by allowing their evolution to be subject to random shocks. As these productivity innovations accumulate over time, they can cause persistent differences across firms. Because we are able to recover the components of productivity for each firm at each point of time, we obtain a detailed assessment of the impact of technological change at the level it takes place, namely the individual firm. In particular, we are able to assess the persistence in the components of productivity and the correlation between them at the level of the individual firm. We are also able to relate the speed and direction of technological change to firms' R&D activities.

To tackle the endogeneity problem in production function estimation, we build on the insight of Olley & Pakes (1996) that if the decisions that a firm makes can be used to infer its productivity, then productivity can be controlled for in the estimation. We extend their insight to a setting in which productivity is multi- instead of single-dimensional. Our starting point is a dynamic model of a firm that is equipped with a CES production function. The model enables us to infer the firm's productivity from its input usage, in particular its labor and materials decisions. As in Doraszelski & Jaumandreu (2013), our estimator exploits the parameter restrictions between the production and input demand functions. This parametric inversion is less demanding on the data than the nonparametric inversion in Olley & Pakes (1996), Levinsohn & Petrin (2003), and Akerberg et al. (2006), especially if the input demand functions are high-dimensional and have many arguments.³

The key insight to identifying the bias of technological change is that Hicks-neutral technological change scales input usage but, in contrast to labor-augmenting technological change, does not change the mix of inputs that a firm uses. A change in the input mix therefore contains information about the bias of technological change, provided we control for the relative prices of the various inputs and other factors that may change the input

³See Doraszelski & Jaumandreu (2013) for details on the pros and cons of the parametric inversion.

mix. Our analysis points to two factors. First, outsourcing directly changes the input mix as the firm procures customized parts and pieces from its suppliers rather than makes them in house from scratch. Second, the Spanish labor market manifestly distinguishes between permanent and temporary labor. We further contribute to the literature following Olley & Pakes (1996) by accounting for the dual nature of the labor market and highlighting the importance of costly adjustments to permanent labor for measuring the bias of technological change.

We apply our estimator to an unbalanced panel of 2375 Spanish manufacturing firms in ten industries from 1990 to 2006. Spain is an attractive setting for examining the speed and direction of technological change for two reasons. First, Spain became fully integrated into the European Union between the end of the 1980s and the beginning of the 1990s. Any trends in technological change that our analysis uncovers for Spain may thus be viewed as broadly representative for other continental European economies. Second, Spain inherited an industrial structure with few high-tech industries and mostly small and medium-sized firms. Traditionally, R&D is viewed as lacking and something to be boosted (OECD 2007). Yet, Spain grew rapidly during the 1990s, and R&D became increasingly important (European Commission 2001). The accompanying changes in industrial structure are a useful source of variation for analyzing the role of R&D in stimulating different types of technological change.

The particular data set we use has several advantages. The broad coverage is unusual and allows us to assess the bias of technological change in industries that differ greatly in terms of firms' R&D activities. The data set also has an unusually long time dimension, enabling us to disentangle trends in technological change from short-term fluctuations. Finally, the data set has firm-level prices that we exploit heavily in the estimation.⁴

Our estimates provide clear evidence that technological change is biased. *Ceteris paribus* labor-augmenting technological change causes output to grow, on average, in the vicinity of 2% per year. While there is a shift from unskilled to skilled workers in our data, this skill upgrading explains some but not all of the growth of labor-augmenting productivity. In many industries, labor-augmenting productivity grows because workers with a given set of skills become more productive over time.

At the same time, our estimates show that Hicks-neutral technological change plays an equally important role. In addition to labor-augmenting technological change, Hicks-neutral technological change causes output to grow, on average, in the vicinity of 2% per year.

Behind these averages lies a substantial amount of heterogeneity across industries and firms. The rates of growth of the components of productivity are positively correlated with their levels, indicating that differences in productivity across firms persist over time.

⁴There are other firm-level data sets such as the Colombian Annual Manufacturers Survey (Eslava, Haltiwanger, Kugler & Kugler 2004) and the Longitudinal Business Database at the U.S. Census Bureau that contain separate information on prices and quantities, at least for a subset of industries (Roberts & Supina 1996, Foster, Haltiwanger & Syverson 2008, Foster, Haltiwanger & Syverson 2013).

Moreover, at the level of the individual firm, the levels of labor-augmenting and Hicks-neutral productivity are positively correlated, as are their rates of growth.

Finally, our estimates indicate that firms' R&D activities are associated with higher levels and rates of growth of labor-augmenting productivity and, perhaps to a lesser extent, with higher levels and rates of growth of Hicks-neutral productivity as well. Firms' R&D activities therefore are important for determining the differences in productivity across firms and the evolution of productivity over time.

Our paper is related to Van Biesebroeck (2003). Using plant-level panel data for the U.S. automobile industry, he estimates Hicks-neutral productivity as a fixed effect and recovers a plant's capital-biased (also called labor-saving) productivity from its input usage. Our approach is similar in that it uses a parametric inversion to recover unobserved productivity from observed inputs. It is more general in that we allow all components of productivity to evolve over time and in response to firms' R&D activities.

Our paper is also related to Grieco, Li & Zhang (2015) who recover multiple unobservables from input usage. Because their data contains the materials bill rather than its split into price and quantity, they infer a firm's Hicks-neutral productivity and the price of materials that the firm faces by parametrically inverting the demand functions for labor and materials. In subsequent work in progress, Zhang (2014*a*, 2014*b*) applies the same idea to recover a firm's capital-augmenting productivity and its labor-augmenting productivity. We return to the related literature in Sections 4 and 7.

Finally, our paper touches—although more tangentially—on the literature on skill bias that studies the differential impact of technological change, especially in the form of computerization, on the various types of labor. Our approach is similar to some of the recent work on skill bias (Machin & Van Reenen 1998, Black & Lynch 2001, Abowd, Haltiwanger, Lane, McKinney & Sandusky 2007, Bloom, Sadun & Van Reenen 2012) in that it starts from a production function and focuses on the individual firm. While we focus on labor versus the other factors of production, the techniques we develop may be adapted to investigate the skill bias of technological change, although our particular data set is not ideal for this purpose. Our approach differs from the recent work on skill bias in that it explicitly models and estimates the differences in productivity across firms and the evolution of firm-level productivity over time. It is also more structural in tackling the endogeneity problem that arises in estimating production functions.

The remainder of this paper is organized as follows: Section 2 describes the data and some patterns in the data that inform the subsequent analysis. Section 3 sets out a dynamic model of the firm. Section 4 develops an estimator for production functions when productivity is multi-dimensional. Sections 5 and 6 describe our main results on labor-augmenting and Hicks-neutral technological change. Section 7 explores whether capital-augmenting technological plays a role in our data in addition to labor-augmenting and Hicks-neutral technological change. Section 8 concludes and outlines directions for future research.

Throughout the paper, we adopt the convention that upper case letters denote levels and lower case letters denote logs. Unless noted otherwise, we refer to output and the various factors of production in terms of quantity and not in terms of value. In particular, we refer to the value of labor as the wage bill and to the value of materials as the materials bill.

2 Data

Our data comes from the Encuesta Sobre Estrategias Empresariales (ESEE) survey, a firm-level survey of the Spanish manufacturing sector sponsored by the Ministry of Industry. The unit of observation is the firm, not the plant or the establishment. Our data covers the 1990s and early 2000s. At the beginning of the survey in 1990, 5% of firms with up to 200 workers were sampled randomly by industry and size strata. All firms with more than 200 workers were asked to participate in the survey and 70% of them complied. Some firms vanish from the sample due to either exit (shutdown by death or abandonment of activity) or attrition. These reasons can be distinguished in the data and attrition remained within acceptable limits. To preserve representativeness, newly created firms were added to the sample every year. We provide details on industry and variable definitions in Appendix A.

Our sample covers a total of 2375 firms in ten industries when restricted to firms with at least three years of data. Columns (1) and (2) of Table 1 show the number of observations and firms by industry. Sample sizes are moderate. Newly created firms are a large fraction of the total number of firms, ranging from 26% to 50% in the different industries. There is a much smaller fraction of exiting firms, ranging from 6% to 15% and above in a few industries. Firms remain in the sample from a minimum of three years to a maximum of 16 years between 1990 and 2006.

The 1990s and early 2000s were a period of rapid output growth, coupled with stagnant or, at best, slightly increasing employment and intense investment in physical capital, see columns (3)–(6) of Table 1. Consistent with this rapid growth, firms on average report that their market is slightly more often expanding rather than contracting; hence, demand tends to shift out over time.

An attractive feature of our data is that it contains firm-specific price indices for output and inputs. The growth of prices, averaged from the growth of prices as reported individually by each firm, is moderate. The growth of the price of output in column (7) ranges from 0.8% to 2.1%. The growth of the wage ranges from 4.3% to 5.4% and the growth of the price of materials ranges from 2.8% to 4.1%.

Biased technological change. The evolution of the relative quantities and prices of the various factors of production already hint at an important role for labor-augmenting technological change. As columns (8) and (9) of Table 1 show, with the exception of

industries 7, 8, and 9, the increase in materials M per unit of labor L is much larger than the decrease in the price of materials P_M relative to the wage W . One possible explanation is that the elasticity of substitution between materials and labor exceeds 1. To see this, recall that the elasticity of substitution is

$$\frac{d \ln \left(\frac{M}{L} \right)}{d \ln \left(\frac{MPR_L}{MPR_M} \right)} = - \frac{d \ln \left(\frac{M}{L} \right)}{d \ln \left(\frac{P_M}{W} \right)},$$

where the equality follows to the extent that the relative marginal products $\frac{MPR_M}{MPR_L}$ equal the relative prices $\frac{P_M}{W}$. However, because the estimates of the elasticity of substitution in the previous literature lie somewhere between 0 and 1 (see Chirinko (2008) and the references therein for the elasticity of substitution between capital and labor and Bruno (1984), Rotemberg & Woodford (1996), and Oberfield & Raval (2014) for the elasticity of substitution between materials and an aggregate of capital and labor), this explanation is implausible. Labor-augmenting technological change offers an alternative explanation. As it makes labor more productive, it directly increases materials per unit of labor (see equation (12) in Section 4). Thus, labor-augmenting technological change may go a long way in rationalizing why the relative quantities $\frac{M}{L}$ change much more than the relative prices $\frac{P_M}{W}$.

In contrast, columns (10) and (11) of Table 1 provide no evidence for capital-augmenting technological change. The investment boom in Spain in the 1990s and early 2000s was fueled by improved access to European and international capital markets. With the exception of industries 5, 6, and 8, the concomitant decrease in materials M per unit of capital K is much smaller than the increase in the price of materials P_M relative to the user cost of capital in our data, a notably rough measure of the price of capital P_K .⁵ This pattern is consistent with an elasticity of substitution between materials and capital between 0 and 1. Indeed, capital-augmenting technological change can only directly contribute to the decline in materials per unit of capital in the unlikely scenario that it makes capital less productive.

Based on these patterns in the data we focus on labor-augmenting technological change in the subsequent analysis. We return to capital-augmenting technological change in Section 7. In the remainder of this section we point out other features of the data that figure prominently in our analysis.

Temporary labor. We treat temporary labor as a static (or “variable”) input that is chosen each period to maximize short-run profits. This is appropriate because Spain greatly enhanced the possibilities for hiring and firing temporary workers during the 1980s and by the beginning of the 1990s had one the highest shares of temporary workers in Europe (Dolado, Garcia-Serrano & Jimeno 2002). Temporary workers are employed for fixed terms

⁵In particular, the price of capital includes adjustment costs, and as a shadow price, it is unobservable. The user cost of capital, in contrast, is based solely on observables (see Appendix A).

with no or very small severance pay. In our sample, between 72% and 84% of firms use temporary labor and among the firms that do its share of the labor force ranges from 16% in industry 10 to 32% in industry 9, see columns (1) and (2) of Table 2.

Rapid expansions and contractions of temporary labor are common: The difference between the maximum and the minimum share of temporary labor within a firm ranges on average from 20% to 33% across industries (column (3)). In addition to distinguishing temporary from permanent labor, we measure labor as hours worked (see Appendix A). At this margin, firms enjoy a high degree of flexibility: Within a firm, the difference between the maximum and the minimum hours worked ranges on average from 43% to 56% across industries, and the difference between the maximum and the minimum hours per worker ranges on average from 4% to 13% (columns (4) and (5)).

Outsourcing. We account for outsourcing in our analysis. Outsourcing may directly contribute to the shift from labor to materials that column (8) of Table 1 documents as firms procure customized parts and pieces from their suppliers rather than make them in house from scratch. As can be seen in columns (6) and (7) of Table 2, between 21% and 57% of firms in our sample engage in outsourcing. Among the firms that do, the share of outsourcing in the materials bill ranges from 14% in industry 7 to 29% in industry 4. While the share of outsourcing remains stable over our sample period, the standard deviation in column (7) indicates a substantial amount of heterogeneity across the firms within an industry, similar to the share of temporary labor in column (2).

Firms' R&D activities. The R&D intensity of Spanish manufacturing firms is low by European standards, but R&D became increasingly important during the 1990s (see, e.g., European Commission 2001).⁶ Columns (8)–(10) of Table 2 show that the ten industries differ markedly in terms of firms' R&D activities and that there is again substantial heterogeneity across the firms within an industry. Industries 3, 4, 5, and 6 exhibit high innovative activity. More than two thirds of firms perform R&D during at least one year in the sample period, with at least 36% of stable performers engaging in R&D in all years (column (8)) and at least 28% of occasional performers engaging in R&D in some but not all years (column (9)). The R&D intensity among performers ranges on average from 2.2% to 2.9% (column (10)). Industries 1, 2, 7, and 8 are in an intermediate position. Less than half of firms perform R&D, and there are fewer stable than occasional performers. The R&D intensity is on average between 1.1% and 1.7% with a much lower value of 0.7% in industry 7. Finally, industries 9 and 10 exhibit low innovative activity. About a third of firms perform R&D, and the R&D intensity is on average between 1.0% and 1.5%.

⁶R&D intensities for manufacturing firms are 2.1% in France, 2.6% in Germany, and 2.2% in the UK as compared to 0.6% in Spain (European Commission 2004).

3 A dynamic model of the firm

Our model builds on the previous literature on the structural estimation of production functions. Its purpose is to enable us to infer a firm’s productivity from its input usage and to clarify our assumptions on the timing of decisions that we rely on in estimation. Olley & Pakes (1996), Levinsohn & Petrin (2003), Akerberg et al. (2006), Doraszelski & Jaumandreu (2013), and many others specify a Cobb-Douglas production function. Productivity is single-dimensional or, equivalently, technological change is Hicks neutral by construction.⁷ To assess the bias of technological change, we generalize the Cobb-Douglas production function and allow productivity to be multi-dimensional.

Production function. The firm has the constant elasticity of substitution (CES) production function

$$Y_{jt} = \beta_0 \left[\beta_K K_{jt}^{-\frac{1-\sigma}{\sigma}} + \beta_L (\exp(\omega_{Ljt}) L_{jt}^*)^{-\frac{1-\sigma}{\sigma}} + \beta_M (M_{jt}^*)^{-\frac{1-\sigma}{\sigma}} \right]^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt}) \exp(e_{jt}), \quad (1)$$

where Y_{jt} is the output of firm j in period t , K_{jt} is capital, $L_{jt}^* = \Lambda(L_{Pjt}, L_{Tjt})$ is an aggregate of permanent labor L_{Pjt} and temporary labor L_{Tjt} , and $M_{jt}^* = \Gamma(M_{Ijt}, M_{Ojt})$ is an aggregate of in-house materials M_{Ijt} and outsourced materials (customized parts and pieces) M_{Ojt} . ω_{Ljt} and ω_{Hjt} are labor-augmenting and Hicks-neutral productivity, respectively, and e_{jt} is a mean zero random shock that is uncorrelated over time and across firms.

The parameters ν and σ are the elasticity of scale and substitution, respectively. Depending on the elasticity of substitution, the production function in equation (1) encompasses the special cases of a Leontieff ($\sigma \rightarrow 0$), Cobb-Douglas ($\sigma = 1$), and linear ($\sigma \rightarrow \infty$) production function. The remaining parameters are the constant of proportionality β_0 and the distributional parameters β_K , β_L , and β_M .⁸ Because β_0 cannot be separated from an additive constant in Hicks-neutral productivity ω_{Hjt} , we estimate them jointly. To simplify the notation and without loss of generality, we set $\beta_0 = 1$ in what follows.⁹ We similarly set $\beta_L = 1$. Viewing technological change as operating by changing the productivities of the various factors of production is therefore equivalent to viewing it as changing these parameters of the production function. Finally, the aggregators $\Lambda(L_{Pjt}, L_{Tjt})$ and $\Gamma(M_{Ijt}, M_{Ojt})$ accommodate differences in the productivities of permanent and temporary labor, respectively, in-house and outsourced materials; we do not further specify these aggregators.

⁷As is well known, a Cobb-Douglas production function has an elasticity of substitution of one and therefore cannot be used to separate different types of technological change. Our data rejects a Cobb-Douglas production function (see Section 5).

⁸Because we are not interested in the economic interpretation of the distributional parameters or in comparative statics with respect to the elasticity of substitution, we do not “normalize” the CES production function (de La Grandville 1989, Klump & de La Grandville 2000).

⁹We carefully ensure that the reported results depend only on the sum of β_0 and the additive constant in Hicks-neutral productivity ω_{Hjt} .

The production function in equation (1) is the most parsimonious we can use to separate labor-augmenting from Hicks-neutral productivity. It encompasses three restrictions. First, technological change does not affect the parameters ν and σ , as we are unaware of evidence suggesting that the elasticity of scale or the elasticity of substitution varies over our sample period. Second, the elasticity of substitution between capital, labor, and materials is the same.¹⁰ This restriction seems sensible to us because previous estimates of the elasticity of substitution between materials and an aggregate of capital and labor (Bruno 1984, Rotemberg & Woodford 1996, Oberfield & Raval 2014) fall in the same range as estimates of the elasticity of substitution between capital and labor (Chirinko 2008).¹¹ Third, the productivities of capital and materials are restricted to change at the same rate and in lockstep with Hicks-neutral technological change.¹² Treating capital and materials the same is in line with the fact that both are, at least to a large extent, produced goods. In contrast, labor is traditionally viewed as unique among the various factors of production,¹³ and changes in its productivity are a tenet of the literature on economic growth. The patterns in the data described in Section 2 further justify focusing on labor-augmenting technological change. In Section 7, we explore more thoroughly whether capital-augmenting technological change plays a role in our data in addition to labor-augmenting and Hicks-neutral technological change.

Laws of motion. The components of productivity are presumably correlated with each other and over time and possibly also correlated across firms. As in Doraszelski & Jaumandreu (2013), we endogenize productivity by incorporating R&D expenditures into the model. To account for nonlinearities and uncertainties in the link between R&D and productivity, we assume that the evolution of the components of productivity is governed by controlled first-order, time-inhomogeneous Markov processes with transition probabilities $P_{L_{t+1}}(\omega_{L_{j,t+1}}|\omega_{L_{j,t}}, R_{j,t})$ and $P_{H_{t+1}}(\omega_{H_{j,t+1}}|\omega_{H_{j,t}}, R_{j,t})$, where $R_{j,t}$ is R&D expenditures. Despite their parsimony, these stochastic processes accommodate correlation between the components of productivity.¹⁴ Moreover, because they are time-inhomogeneous, they ac-

¹⁰The elasticity of substitution between $L_{P_{j,t}}$ and $L_{T_{j,t}}$, respectively, $M_{I_{j,t}}$ and $M_{O_{j,t}}$ depends on the aggregators $\Lambda(L_{P_{j,t}}, L_{T_{j,t}})$ and $\Gamma(M_{I_{j,t}}, M_{O_{j,t}})$ and may differ from σ .

¹¹Our empirical strategy generalizes to a nested CES and translog production function, although some nestings require numerically solving a system of equations to infer unobservables from observables.

¹²A production function with capital-augmenting, labor-augmenting, and materials-augmenting productivity that is homogeneous of arbitrary degree is equivalent to a production function with capital-augmenting, labor-augmenting, and Hicks-neutral productivity. Without loss of generality, we therefore subsume the common component of capital-augmenting, labor-augmenting, and materials-augmenting technological change into Hicks-neutral productivity.

¹³Marshall (1920), for example, writes in great detail about the variability of workers' efforts and its relationship to productivity.

¹⁴Our empirical strategy generalizes to a joint Markov process $P_{t+1}(\omega_{L_{j,t+1}}, \omega_{H_{j,t+1}}|\omega_{L_{j,t}}, \omega_{H_{j,t}}, r_{j,t})$. While R&D is widely seen as a major source of productivity growth (see Griliches (1998, 2000) for surveys of the empirical literature), our empirical strategy extends to other sources such as technology adoption. Our data has investment in computer equipment and indicators of whether a firm has adopted digitally controlled machine tools, CAD, and robots. Both extensions are demanding on the data, however, as they increase the

commodate secular trends in productivity.

The firm knows its current productivity when it makes its decisions for period t and anticipates the effect of R&D on its future productivity. The Markovian assumption implies

$$\omega_{Ljt+1} = E_t[\omega_{Ljt+1}|\omega_{Ljt}, R_{jt}] + \xi_{Ljt+1} = g_{Lt}(\omega_{Ljt}, R_{jt}) + \xi_{Ljt+1}, \quad (2)$$

$$\omega_{Hjt+1} = E_t[\omega_{Hjt+1}|\omega_{Hjt}, R_{jt}] + \xi_{Hjt+1} = g_{Ht}(\omega_{Hjt}, R_{jt}) + \xi_{Hjt+1}. \quad (3)$$

That is, *actual* labor-augmenting productivity ω_{Ljt+1} in period $t + 1$ decomposes into *expected* labor-augmenting productivity $g_{Lt}(\omega_{Ljt}, R_{jt})$ and a random shock ξ_{Ljt+1} . This *productivity innovation* is by construction mean independent (although not necessarily fully independent) of ω_{Ljt} and R_{jt} . It captures the uncertainties that are naturally linked to productivity as well as those that are inherent in the R&D process such as chance of discovery, degree of applicability, and success in implementation. Nonlinearities in the link between R&D and productivity are captured by the conditional expectation function $g_{Lt}(\cdot)$ that we estimate nonparametrically along with the parameters of the production function. Actual Hicks-neutral productivity ω_{Hjt+1} decomposes similarly.

Capital accumulates according to $K_{jt+1} = (1 - \delta)K_{jt} + I_{jt}$, where δ is the rate of depreciation. As in Olley & Pakes (1996), investment I_{jt} chosen in period t becomes effective in period $t + 1$. Choosing I_{jt} is therefore equivalent to choosing K_{jt+1} .

In recognition of the dual nature of the labor market in Spain, we distinguish between permanent and temporary labor. Permanent labor is subject to convex adjustment costs $C_{Lp}(LP_{jt}, LP_{jt-1})$ that reflect the substantial cost of hiring and firing that the firm may incur (Hammermesh 1993, Hammermesh & Pfann 1996). The choice of permanent labor thus may have dynamic implications. In contrast, temporary labor is a static input.

We further distinguish between in-house and outsourced materials. Outsourcing is, to a large extent, based on contractual relationships between the firm and its suppliers (Grossman & Helpman 2002, Grossman & Helpman 2005). The ratio of outsourced to in-house materials $Q_{Mjt} = \frac{M_{Ojt}}{M_{Ijt}}$ is subject to (convex or not) adjustment costs $C_{Q_M}(Q_{Mjt+1}, Q_{Mjt})$ that stem from forming and dissolving these relationships. The firm must maintain Q_{Mjt} but may scale M_{Ijt} and M_{Ojt} up or down at will; in-house materials, in particular, is a static input. In the Online Appendix, we develop an alternative model of outsourcing that assumes that both in-house and outsourced materials are static inputs that the firm may mix-and-match at will, thereby dispensing with the costly-to-adjust ratio of outsourced to in-house materials.

Output and input markets. The firm has market power in the output market, e.g., because products are differentiated. Its inverse residual demand function $P(Y_{jt}, D_{jt})$ depends

dimensionality of the functions that must be nonparametrically estimated.

on its output Y_{jt} and the demand shifter D_{jt} .¹⁵ The firm is a price-taker in input markets, where it faces W_{Pjt} , W_{Tjt} , P_{Ijt} , and P_{Ojt} as prices of permanent and temporary labor and in-house and outsourced materials, respectively. In Section 5 we instead assume that the firm faces a menu of qualities and wages in the market for permanent labor.

The demand shifter and the prices that the firm faces in input markets evolve according to a Markov process that we do not further specify. As a consequence, the prices that the firm faces in period $t+1$ may depend on its productivity in period t or on an average industry-wide measure of productivity. Finally, the Markov process may be time-inhomogenous to accommodate secular trends.

Bellman equation. The firm makes its decisions in a discrete time setting with the goal of maximizing the expected net present value of future cash flows. In contrast to its labor-augmenting productivity ω_{Ljt} and its Hicks-neutral productivity ω_{Hjt} , the firm does not know the random shock e_{jt} when it makes its decisions for period t . Letting $V_t(\cdot)$ denote the value function in period t , the Bellman equation for the firm's dynamic programming problem is

$$\begin{aligned}
V_t(\Omega_{jt}) = & \max_{K_{jt+1}, L_{Pjt}, L_{Tjt}, Q_{Mjt+1}, M_{Ijt}, R_{jt}} P \left(X_{jt}^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt}), D_{jt} \right) X_{jt}^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt}) \mu \\
& - C_I(K_{jt+1} - (1 - \delta)K_{jt}) - W_{Pjt}L_{Pjt} - C_{LP}(L_{Pjt}, L_{Pjt-1}) - W_{Tjt}L_{Tjt} \\
& - (P_{Ijt} + P_{Ojt}Q_{Mjt})M_{Ijt} - C_{QM}(Q_{Mjt+1}, Q_{Mjt}) - C_R(R_{jt}) \\
& + \frac{1}{1 + \rho} E_t [V_{t+1}(\Omega_{jt+1}) | \Omega_{jt}, R_{jt}], \tag{4}
\end{aligned}$$

where

$$X_{jt} = \beta_K K_{jt}^{-\frac{1-\sigma}{\sigma}} + (\exp(\omega_{Ljt})L_{jt}^*)^{-\frac{1-\sigma}{\sigma}} + \beta_M (M_{jt}^*)^{-\frac{1-\sigma}{\sigma}}, \quad \mu = E_t [\exp(e_{jt})],$$

$\Omega_{jt} = (K_{jt}, L_{Pjt-1}, Q_{Mjt}, \omega_{Ljt}, \omega_{Hjt}, W_{Pjt}, W_{Tjt}, P_{Ijt}, P_{Ojt}, D_{jt})$ is the vector of state variables, and ρ is the discount rate. $C_I(I_{jt})$ and $C_R(R_{jt})$ are the cost of investment and R&D, respectively, and accommodate indivisibilities in investment and R&D projects. The firm's dynamic programming problem gives rise to policy functions that characterize its investment and R&D decisions (and thus the values of K_{jt+1} or, equivalently, I_{jt} and R_{jt} in period t) as well as its input usage (L_{Pjt} , L_{Tjt} , Q_{Mjt+1} , and M_{Ijt}). The latter is central to our empirical strategy.

Investment and R&D decisions. The investment and R&D decisions depend on the vector of state variables in our model. In the spirit of the literature on induced innovation and directed technical change (Hicks 1932, Acemoglu 2002), the firm may account for current

¹⁵In general, the residual demand that the firm faces depends on its rivals' prices. In taking the model to the data, one may replace rivals' prices by an aggregate price index or dummies, although this substantially increases the dimensionality of the functions that must be nonparametrically estimated.

input prices (as they are part of Ω_{jt}) and its expectation of future input prices (through the continuation value in equation (4)).¹⁶

Input usage. We infer the firm's productivity from its labor and materials decisions. The first-order conditions for permanent and temporary labor are

$$\nu\mu X_{jt}^{-\left(1+\frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma}\omega_{Ljt}\right) (L_{jt}^*)^{-\frac{1}{\sigma}} \frac{\partial L_{jt}^*}{\partial L_{Pjt}} = \frac{W_{Pjt}(1+\Delta_{jt})}{P_{jt}\left(1-\frac{1}{\eta(p_{jt},D_{jt})}\right)}, \quad (5)$$

$$\nu\mu X_{jt}^{-\left(1+\frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma}\omega_{Ljt}\right) (L_{jt}^*)^{-\frac{1}{\sigma}} \frac{\partial L_{jt}^*}{\partial L_{Tjt}} = \frac{W_{Tjt}}{P_{jt}\left(1-\frac{1}{\eta(p_{jt},D_{jt})}\right)}, \quad (6)$$

where $\eta(p_{jt}, D_{jt})$ is the absolute value of the price elasticity of the residual demand that the firm faces, and by the envelope theorem, the gap between the wage of permanent workers W_{Pjt} and the shadow wage is

$$\begin{aligned} \Delta_{jt} &= \frac{1}{W_{Pjt}} \left(\frac{\partial C_{LP}(L_{Pjt}, L_{Pjt-1})}{\partial L_{Pjt}} - \frac{1}{1+\rho} E_t \left[\frac{\partial V_{t+1}(\Omega_{jt+1})}{\partial L_{Pjt}} | \Omega_{jt}, R_{jt} \right] \right) \\ &= \frac{1}{W_{Pjt}} \left(\frac{\partial C_{LP}(L_{Pjt}, L_{Pjt-1})}{\partial L_{Pjt}} + \frac{1}{1+\rho} E_t \left[\frac{\partial C_{LP}(L_{Pjt+1}, L_{Pjt})}{\partial L_{Pjt}} | \Omega_{jt}, R_{jt} \right] \right). \end{aligned}$$

Equations (5) and (6) allow the mix of permanent and temporary labor to depend on the firm's productivity and the other state variables (through Δ_{jt}).

Our data combines the wages of permanent and temporary workers into $W_{jt} = W_{Pjt}(1 - S_{Tjt}) + W_{Tjt}S_{Tjt}$, where $S_{Tjt} = \frac{L_{Tjt}}{L_{jt}}$ is the (quantity) share of temporary labor and $L_{jt} = L_{Pjt} + L_{Tjt}$ is hours worked by permanent and temporary workers in our data. To make do, we assume that the aggregator $\Lambda(L_{Pjt}, L_{Tjt})$ is linearly homogenous. This implies $L_{jt}^* = L_{jt}\Lambda(1 - S_{Tjt}, S_{Tjt})$, $\frac{\partial L_{jt}^*}{\partial L_{Pjt}} = \Lambda_P(1 - S_{Tjt}, S_{Tjt})$, and $\frac{\partial L_{jt}^*}{\partial L_{Tjt}} = \Lambda_T(1 - S_{Tjt}, S_{Tjt})$. Using Euler's theorem to combine equations (5) and (6) yields

$$\begin{aligned} &\nu\mu X_{jt}^{-\left(1+\frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma}\omega_{Ljt}\right) L_{jt}^{-\frac{1}{\sigma}} \Lambda(1 - S_{Tjt}, S_{Tjt})^{-\frac{1-\sigma}{\sigma}} \\ &= \frac{W_{jt} \left(1 + \frac{\Delta_{jt}}{\frac{W_{Tjt} S_{Tjt}}{1 + \frac{W_{Pjt}}{W_{Tjt}}(1 - S_{Tjt})}} \right)}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})} \right)} = \frac{W_{jt} \left(\frac{\frac{\Lambda_P(1 - S_{Tjt}, S_{Tjt})}{\Lambda_T(1 - S_{Tjt}, S_{Tjt})} + \frac{S_{Tjt}}{1 - S_{Tjt}}}{\frac{W_{Pjt}}{W_{Tjt}} + \frac{S_{Tjt}}{1 - S_{Tjt}}} \right)}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})} \right)}, \quad (7) \end{aligned}$$

where the second equality follows from dividing equations (5) and (6) and solving for Δ_{jt} .

Because our data does not have the ratio $\frac{W_{Pjt}}{W_{Tjt}}$, we assume that $\frac{W_{Pjt}}{W_{Tjt}} = \lambda_0$ is an (un-

¹⁶The firm may further account for its expectation of future output demand and input supply conditions. Because our empirical strategy infers the firm's productivity from its labor and materials decisions, it is not affected by including additional state variables to model the evolution of these conditions in our model besides the demand shifter D_{jt} .

known) constant¹⁷ and treat $\frac{\frac{\lambda_P(1-S_{Tjt}, S_{Tjt})}{\lambda_T(1-S_{Tjt}, S_{Tjt})} + \frac{S_{Tjt}}{1-S_{Tjt}}}{\lambda_0 + \frac{S_{Tjt}}{1-S_{Tjt}}} = \lambda_1(S_{Tjt})$ as an (unknown) function of S_{Tjt} that must be estimated nonparametrically along with the parameters of the production function. Because equation (7) presumes interior solutions for permanent and temporary labor, we exclude observations with $S_{Tjt} = 0$ and thus $L_{Tjt} = 0$ from the subsequent analysis.¹⁸

Turning from the labor to the materials decision, because the firm must maintain the ratio of outsourced to in-house materials Q_{Mjt} , the first-order condition for in-house materials is

$$\nu\beta_M\mu X_{jt}^{-(1+\frac{\nu\sigma}{1-\sigma})} \exp(\omega_{Hjt}) (M_{jt}^*)^{-\frac{1}{\sigma}} \frac{dM_{jt}^*}{dM_{Ijt}} = \frac{P_{Ijt} + P_{Ojt}Q_{Mjt}}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)}, \quad (8)$$

where $P_{Ijt} + P_{Ojt}Q_{Mjt}$ is the effective cost of an additional unit of in-house materials.

Our data has the materials bill $P_{Mjt}M_{jt} = P_{Ijt}M_{Ijt} + P_{Ojt}M_{Ojt}$, the (value) share of outsourced materials $S_{Ojt} = \frac{P_{Ojt}M_{Ojt}}{P_{Mjt}M_{jt}}$, and the price of materials P_{Mjt} . We assume $P_{Mjt} = P_{Ijt} + P_{Ojt}Q_{Mjt}$ so that the price of materials is the effective cost of an additional unit of in-house materials. This implies $M_{jt} = M_{Ijt}$. To map the model to the data, we further assume that $\Gamma(M_{Ijt}, M_{Ojt})$ is linearly homogenous and normalize $\Gamma(M_{Ijt}, 0) = M_{Ijt}$. This implies $M_{jt}^* = M_{Ijt}\Gamma\left(1, \frac{P_{Ijt}}{P_{Ojt}}\frac{S_{Ojt}}{1-S_{Ojt}}\right)$ and $\frac{dM_{jt}^*}{dM_{Ijt}} = \Gamma\left(1, \frac{P_{Ijt}}{P_{Ojt}}\frac{S_{Ojt}}{1-S_{Ojt}}\right)$. Rewriting equation (8) yields

$$\nu\beta_M\mu X_{jt}^{-(1+\frac{\nu\sigma}{1-\sigma})} \exp(\omega_{Hjt}) M_{jt}^{-\frac{1}{\sigma}} \Gamma\left(1, \frac{P_{Ijt}}{P_{Ojt}}\frac{S_{Ojt}}{1-S_{Ojt}}\right)^{-\frac{1-\sigma}{\sigma}} = \frac{P_{Mjt}}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)}. \quad (9)$$

Because our data does not have the ratio $\frac{P_{Ijt}}{P_{Ojt}}$, we assume that $\frac{P_{Ijt}}{P_{Ojt}} = \gamma_0$ is an (unknown) constant and treat $\ln \Gamma\left(1, \gamma_0\frac{S_{Ojt}}{1-S_{Ojt}}\right) = \gamma_1(S_{Ojt})$ as an (unknown) function of S_{Ojt} .¹⁹ Equation (9) presumes an interior solution for in-house materials; it is consistent with a corner solution for outsourced materials. Indeed, absent outsourcing equation (9) reduces to the first-order condition for in-house materials.

Our primary interest is the bias of technological change. We thus think of $\lambda_1(S_{Tjt})$

¹⁷In Appendix D, we use a wage regression to estimate wage premia of various types of labor. In the Online Appendix, we extend the specification and demonstrate that the wage premia do not change much if at all over time in line with our assumption that the ratio $\frac{W_{Pjt}}{W_{Ljt}}$ is constant.

¹⁸Compare columns (1) and (2) of Tables 1 and 3 with columns (1) and (2) of Table 4 for the exact number of observations and firms we exclude.

¹⁹We have experimented with assuming that $\frac{P_{Ijt}}{P_{Ojt}} = \gamma_0(t)$ is an (unknown) function of time t and treating $\ln \Gamma\left(1, \gamma_0(t)\frac{S_{Ojt}}{1-S_{Ojt}}\right) = \gamma_1\left(\gamma_0(t)\frac{S_{Ojt}}{1-S_{Ojt}}\right)$ as an (unknown) function of $\gamma_0(t)S_{Ojt}$. As we show in the Online Appendix, not much changes. Equation (13) tends to yield somewhat lower estimates of σ compared to our leading estimates in column (3) of Table 4. Compared to our leading estimates in columns (1) and (2) of Table 6 equation (16) tends to yield somewhat lower estimates of β_K and similar estimates of ν in the eight industries where we have been able to obtain estimates. Our conclusions about technological change remain the same.

and $\gamma_1(S_{Ojt})$ as “correction terms” on labor and, respectively, materials that help account for the substantial heterogeneity across the firms within an industry. Because we estimate these terms nonparametrically, they can accommodate different theories about the Spanish labor market and the role of outsourcing. For example, we develop an alternative model of outsourcing in the Online Appendix that assumes that both in-house and outsourced materials are static inputs that the firm may mix-and-match at will.

Productivity. From the labor and materials decisions in equations (7) and (9) we recover (conveniently rescaled) labor-augmenting productivity $\tilde{\omega}_{Ljt} = (1 - \sigma)\omega_{Ljt}$ and Hicks-neutral productivity ω_{Hjt} as

$$\begin{aligned}\tilde{\omega}_{Ljt} &= \tilde{\gamma}_L + m_{jt} - l_{jt} + \sigma(p_{Mjt} - w_{jt}) - \sigma\lambda_2(S_{Tjt}) + (1 - \sigma)\gamma_1(S_{Ojt}) \\ &\equiv \tilde{h}_L(m_{jt} - l_{jt}, p_{Mjt} - w_{jt}, S_{Tjt}, S_{Ojt}),\end{aligned}\tag{10}$$

$$\begin{aligned}\omega_{Hjt} &= \gamma_H + \frac{1}{\sigma}m_{jt} + p_{Mjt} - p_{jt} - \ln\left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right) \\ &\quad + \left(1 + \frac{\nu\sigma}{1 - \sigma}\right)x_{jt} + \frac{1 - \sigma}{\sigma}\gamma_1(S_{Ojt}) \\ &\equiv h_H(k_{jt}, m_{jt}, S_{Mjt}, p_{jt}, p_{Mjt}, D_{jt}, S_{Tjt}, S_{Ojt}),\end{aligned}\tag{11}$$

where $\tilde{\gamma}_L = -\sigma \ln \beta_M$, $\lambda_2(S_{Tjt}) = \ln\left(\lambda_1(S_{Tjt})\Lambda(1 - S_{Tjt}, S_{Tjt})^{\frac{1-\sigma}{\sigma}}\right)$, $\gamma_H = -\ln(\nu\beta_M\mu)$,

$$X_{jt} = \beta_K K_{jt}^{-\frac{1-\sigma}{\sigma}} + \beta_M (M_{jt} \exp(\gamma_1(S_{Ojt})))^{-\frac{1-\sigma}{\sigma}} \left(\frac{1 - S_{Mjt}}{S_{Mjt}} \lambda_1(S_{Tjt}) + 1\right),$$

and $S_{Mjt} = \frac{P_{Mjt}M_{jt}}{W_{jt}L_{jt} + P_{Mjt}M_{jt}}$ is the share of materials in variable cost. Recall that upper case letters denote levels and lower case letters denote logs. The functions $\tilde{h}_L(\cdot)$ and $h_H(\cdot)$ allow us to recover unobservable labor-augmenting productivity $\tilde{\omega}_{Ljt}$ and Hicks-neutral productivity ω_{Hjt} from observables, and we refer to them as inverse functions from hereon. Without loss of generality, we set $\beta_K + \beta_M = 1$.

The inverse function in equation (10) captures the intuition that the mix of inputs that a firm uses is related to—and therefore contains information about—its labor-augmenting productivity but is unrelated to its Hicks-neutral productivity. To see this, note that equation (10) is the (log of the) ratio of the labor and materials decisions in equations (7) and (9) and that these decisions hinge on the marginal products of labor and materials. Because the marginal products are proportional to Hicks-neutral productivity, materials per unit of labor as determined by the ratio of equations (7) and (9) is unrelated to Hicks-neutral productivity, provided we control for outsourcing and adjustment costs on permanent labor.

4 Empirical strategy

The endogeneity problem in production function estimation arises because a firm’s decisions depend on its productivity, and productivity is not observed by the econometrician. However, if the firm’s productivity can be inferred from its decisions, then it can be controlled for in the estimation. To do so, we combine the inverse functions in equations (10) and (11) with the laws of motion for labor-augmenting and Hicks-neutral productivity in equations (2) and (3) into estimation equations for the parameters of the production function in equation (1).

To motivate our empirical strategy and relate it to the literature, it is helpful to abstract from the distinction between permanent and temporary labor and in-house and outsourced materials. To this end, we follow Levinsohn & Petrin (2003) and assume that labor l_{jt} and materials m_{jt} are homogenous inputs that are chosen each period to maximize short-run profits.²⁰ This implies $\lambda_1(S_{Tjt}) = 1$, $\lambda_2(S_{Tjt}) = 0$, and $\gamma_1(S_{Ojt}) = 0$, so that the simplified model emerges as a special case as the correction terms on labor and materials vanish.

In the simplified model, equation (10) can be rewritten as

$$m_{jt} - l_{jt} = -\tilde{\gamma}_L - \sigma(p_{Mjt} - w_{jt}) + \tilde{\omega}_{Ljt}. \quad (12)$$

Equation (12) shows that materials per unit of labor varies over time and across firms for two reasons. First, it varies according to the price of materials p_{Mjt} relative to the price of labor w_{jt} . For example, if the relative price of materials falls, then materials per unit of labor rises. Second, labor-augmenting technological change increases materials per unit of labor. A rise in $\tilde{\omega}_{Ljt}$ ceteris paribus causes a rise in materials per unit of labor. This reflects the displacement effect of labor-augmenting technological change.

Related literature. Equation (12) with skilled and unskilled workers in place of materials and labor is at the heart of the literature on skill bias (see Card & DiNardo (2002) and Violante (2008) and the references therein); with capital in place of materials, equation (12) serves to estimate the elasticity of substitution σ in an aggregate value-added production function (see Antràs 2004).

Equation (12) is often estimated by OLS. The problem is that labor-augmenting productivity, which is not observed by the econometrician, is correlated over time and also with the wage. Even though the firm takes W_{Pjt} and W_{Tjt} as given in our model, the wage $w_{jt} = \ln(W_{Pjt}(1 - S_{Tjt}) + W_{Tjt}S_{Tjt})$ may depend on the firm’s productivity via the share of temporary labor S_{Tjt} (see again equations (5) and (6)). Intuitively, we expect the wage to be higher when labor is more productive, even if it adjusts slowly with some lag. This

²⁰Levinsohn & Petrin (2003) invoke this assumption to establish in their equation (9) a sufficient condition for the invertibility of the intermediate input: On p. 320, just below equation (1), they assume that labor is “freely variable,” on p. 322, just above equation (6), they assume that the intermediate input is also “freely variable,” and they invoke short-run profit maximization at the start of the proof on p. 339.

positive correlation induces an upward bias in the estimate of the elasticity of substitution. This is a variant of the endogeneity problem in production function estimation.

It is widely recognized that the estimate of the elasticity of substitution may be biased as a result. Proxying for unobserved productivity by a time trend, time dummies, or a measure of innovation is unlikely to completely remove the bias. Antràs (2004) shows that the estimate of the elasticity of substitution improves by including a time trend and allowing for serial correlation in the remaining error term. However, less than fully accounting for the evolution of productivity leaves an error term that likely remains correlated with the ratio of prices. Using firm-level panel data, Van Reenen (1997) proxies for unobserved productivity by the number of innovations commercialized in a given year. His approach assumes that the remaining error term is white noise and is thus unlikely to succeed if productivity is governed by a more general stochastic process.²¹ Also using firm-level panel data, Raval (2013) estimates the elasticity of substitution in a variant of equation (12) obtained from a value-added production function with capital- and labor-augmenting productivity.²² This rests on the assumption that capital and labor are both static inputs that are chosen each period to maximize short-run profits.²³ Proxying for the firm-specific wage by a regional wage index and for the price of capital by a dummy, Raval (2013) runs OLS by year and sometimes by industry. While not using time-series variation may alleviate the endogeneity problem, relying on proxies introduces measurement error as a source of bias.

Labor-augmenting productivity. Instead of directly estimating a relationship like equation (12), we use equation (10) to recover labor-augmenting productivity $\tilde{\omega}_{Ljt}$ and equation (2) to model its evolution. Substituting the inverse function in equation (10) into the law of motion in equation (2), we form our first estimation equation

$$m_{jt} - l_{jt} = -\sigma(p_{Mjt} - w_{jt}) + \sigma\lambda_2(S_{Tjt}) - (1 - \sigma)\gamma_1(S_{Ojt}) + \tilde{g}_{Lt-1}(\tilde{h}_L(m_{jt-1} - l_{jt-1}, p_{Mjt-1} - w_{jt-1}, S_{Tjt-1}, S_{Ojt-1}), R_{jt-1}) + \tilde{\xi}_{Ljt}, \quad (13)$$

where the (conveniently rescaled) conditional expectation function is

$$\tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1}) = (1 - \sigma)g_{Lt-1}\left(\frac{\tilde{h}_L(\cdot)}{1 - \sigma}, R_{jt-1}\right)$$

²¹Indeed, Van Reenen (1997) obtains a positive direct effect of innovation on employment, contrary to the displacement effect of labor-augmenting technological change.

²²See Gandhi et al. (2013) for a recent discussion of the drawbacks of estimating a value-added instead of a gross-output production function.

²³In contrast, the literature following Olley & Pakes (1996) stresses that the choice of capital has dynamic implications.

and $\tilde{\xi}_{Ljt} = (1 - \sigma)\xi_{Ljt}$.²⁴ Compared to equation (12), equation (13) intuitively diminishes the endogeneity problem because breaking out the part of $\tilde{\omega}_{Ljt}$ that is observable via the conditional expectation function $\tilde{g}_{Lt-1}(\cdot)$ leaves “less” in the error term. As discussed below, equation (13) also facilitates instrumenting for any remaining correlation between the included variables and the error term.

In estimating equation (13), we allow $\tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1})$ to differ between zero and positive R&D expenditures and specify

$$\begin{aligned} \tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1}) &= \tilde{g}_{L0}(t-1) + 1(R_{jt-1} = 0)\tilde{g}_{L1}(\tilde{h}_L(\cdot)) \\ &\quad + 1(R_{jt-1} > 0)\tilde{g}_{L2}(\tilde{h}_L(\cdot), r_{jt-1}), \end{aligned} \quad (14)$$

where $1(\cdot)$ is the indicator function and the functions $\tilde{g}_{L1}(\tilde{h}_L(\cdot))$ and $\tilde{g}_{L2}(\tilde{h}_L(\cdot), r_{jt-1})$ are modeled as described in Appendix B. Because the Markov processes governing productivity is time-inhomogeneous, we allow the conditional expectation function $\tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1})$ to shift over time by $\tilde{g}_{L0}(t-1)$. In practice, we model this shift with time dummies.

As discussed above, labor l_{jt} , materials m_{jt} , the wage w_{jt} , and the share of temporary labor S_{Tjt} are correlated with $\tilde{\xi}_{Ljt}$ in our model (since $\tilde{\xi}_{Ljt}$ is part of $\tilde{\omega}_{Ljt}$). We therefore base estimation on the moment conditions

$$E \left[A_{Ljt}(z_{jt})\tilde{\xi}_{Ljt} \right] = 0, \quad (15)$$

where $A_{Ljt}(z_{jt})$ is a vector of functions of the exogenous variables z_{jt} as described in Appendix B.

In considering instruments it is important to keep in mind that equation (13) models the evolution of labor-augmenting productivity $\tilde{\omega}_{Ljt}$. As a consequence, instruments have to be uncorrelated with the productivity innovation $\tilde{\xi}_{Ljt}$ but not necessarily with productivity itself. Because $\tilde{\xi}_{Ljt}$ is the innovation to productivity $\tilde{\omega}_{Ljt}$ in period t , it is not known to the firm when it makes its decisions in period $t-1$. All past decisions are therefore uncorrelated with $\tilde{\xi}_{Ljt}$. In particular, having been decided in period $t-1$, l_{jt-1} and m_{jt-1} are uncorrelated with $\tilde{\xi}_{Ljt}$, although they are correlated with $\tilde{\omega}_{Ljt}$ as long as productivity is correlated over time. Similarly, because S_{Tjt-1} and thus $w_{jt-1} = \ln(W_{Pjt-1}(1 - S_{Tjt-1}) + W_{Tjt-1}S_{Tjt-1})$ are determined in period $t-1$, they are uncorrelated with the productivity innovation $\tilde{\xi}_{Ljt}$ in period t . We therefore use lagged labor l_{jt-1} , lagged materials m_{jt-1} , and the lagged wage w_{jt-1} for instruments.

In our model, the price of materials $p_{Mjt} = \ln(P_{Ijt} + P_{Ojt}Q_{Mjt})$ is uncorrelated with $\tilde{\xi}_{Ljt}$ because the ratio of outsourced to in-house materials Q_{Mjt} is determined in period $t-1$. For the same reason, the share of outsourced materials $S_{Ojt} = \frac{P_{Ojt}Q_{Mjt}}{P_{Ijt} + P_{Ojt}Q_{Mjt}}$ is uncorrelated

²⁴Equation (13) is a semiparametric, partially linear, model with the additional restriction that the inverse function $\tilde{h}_L(\cdot)$ is of known form. Identification in the sense of the ability to separate the parametric and nonparametric parts of the model follows from standard arguments (Robinson 1988, Newey, Powell & Vella 1999).

with $\tilde{\xi}_{Ljt}$. We nevertheless choose to err on the side of caution and restrict ourselves to the lagged price of materials p_{Mjt-1} and the lagged share of outsourcing S_{Ojt-1} for instruments in light of the reasoning underlying Olley & Pakes (1996), Levinsohn & Petrin (2003), and Akerberg et al. (2006) that lagged values are less susceptible to endogeneity than current values. Finally, time t and the demand shifter D_{jt} are exogenous by construction and we use them for instruments.

A test for overidentifying restrictions in Section 5 cannot reject the validity of the moment conditions in equation (15). As discussed there, this is because the aggregators $\Lambda(L_{Pjt}, L_{Tjt})$ and $\Gamma(M_{Ijt}, M_{Ojt})$ and the correction terms $\lambda_2(S_{Tjt})$ and $\gamma_1(S_{Ojt})$ associated with them account for quality differences between permanent and temporary labor, respectively, in-house and outsourced materials and differences in the use of these inputs over time and across firms.

To the extent that a concern remains, it must thus draw on the notion that quality differences at a finer level play an important role. We address this concern in two ways by leveraging our data on the skill mix of a firm’s labor force. First, in our data the larger part of the variation in the wage across firms and periods can be attributed to geographic and temporal differences in the supply of labor and the fact that firms operate in different product submarkets (see Appendix D). This part of the variation is arguably exogenous and therefore useful for estimating equation (13). The smaller part of the variation in the wage can be attributed to differences in the skill mix and the quality of labor that may potentially be correlated with the error term in equation (13).²⁵ However, we show in Section 5 that our estimates are robust to purging the variation due to differences in the skill mix from the lagged wage w_{jt-1} . Second, in Section 5 we explicitly model quality differences at a finer level by assuming that the firm faces a menu of qualities and wages in the market for permanent labor.

Hicks-neutral productivity. Substituting the inverse functions in equations (10) and (11) into the production function in equation (1) and the law of motion for Hicks-neutral

²⁵A parallel discussion applies to materials. Kugler & Verhoogen (2012) point to differences in the quality of materials whereas Atalay (2014) documents substantial variation in the price of materials across plants in narrowly defined industries with negligible quality differences. This variation is partly due to geography and differences in cost and markup across suppliers that are arguably exogenous to a plant.

productivity ω_{Hjt} in equation (3), we form our second estimation equation^{26,27}

$$y_{jt} = -\frac{\nu\sigma}{1-\sigma}x_{jt} + g_{Ht-1}(h_H(k_{jt-1}, m_{jt-1}, S_{Mjt-1}, p_{jt-1}, p_{Mjt-1}, D_{jt-1}, S_{Tjt-1}, S_{Ojt-1}), R_{jt-1}) + \xi_{Hjt} + e_{jt}. \quad (16)$$

We specify $g_{Ht-1}(h_H(\cdot), R_{jt-1})$ analogously to $\tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1})$ in equation (14).

Because output y_{jt} , materials m_{jt} , the share of materials in variable cost S_{Mjt} , and the share of temporary labor S_{Tjt} are correlated with ξ_{Hjt} , we base estimation on the moment conditions

$$E [A_{Hjt}(z_{jt})(\xi_{Hjt} + e_{jt})] = 0,$$

where $A_{Hjt}(z_{jt})$ is a vector of function of the exogenous variables z_{jt} . As before, we exploit the timing of decisions to rely on lags for instruments. In addition, $k_{jt} = \ln((1-\delta)K_{jt-1} + I_{jt-1})$ is determined in period $t-1$ and therefore uncorrelated with ξ_{Hjt} .

Estimation. We use the two-step GMM estimator of Hansen (1982). Let $\nu_{Ljt}(\theta_L) = \tilde{\xi}_{Ljt}$ be the residual of estimation equation (13) as a function of the parameters θ_L to be estimated and $\nu_{Hjt}(\theta_H) = \xi_{Hjt} + e_{jt}$ the residual of estimation equation (16) as a function of θ_H . The GMM problem corresponding to equation (13) is

$$\min_{\theta_L} \left[\frac{1}{N} \sum_j A_{Lj}(z_j) \nu_{Lj}(\theta_L) \right]' \widehat{W}_L \left[\frac{1}{N} \sum_j A_{Lj}(z_j) \nu_{Lj}(\theta_L) \right], \quad (17)$$

where $A_{Lj}(z_j)$ is a $Q_L \times T_j$ matrix of functions of the exogenous variables z_j , $\nu_{Lj}(\theta_L)$ is a $T_j \times 1$ vector, \widehat{W}_L is a $Q_L \times Q_L$ weighting matrix, Q_L is the number of instruments, T_j is the number of observations of firm j , and N is the number of firms. We provide further details in Appendix B.

The GMM problem corresponding to equation (16) is analogous. Equation (16) is considerably more nonlinear than equation (13). To facilitate its estimation, we impose the estimated values of those parameters in θ_L that also appear in θ_H . We correct the standard errors as described in the Online Appendix. Because they tend to be more stable, we report first-step estimates for equation (16) and use them in the subsequent analysis; however, we use second-step estimates for testing.

²⁶There are other possible estimation equations. In particular, one can use the labor and materials decisions in equations (7) and (9) together with the production function in equation (1) to recover $\tilde{\omega}_{Ljt}$, ω_{Hjt} , and e_{jt} and then set up separate moment conditions in $\tilde{\xi}_{Ljt}$, ξ_{Hjt} , and e_{jt} . This may yield efficiency gains. Our estimation equation (16) has the advantage that it is similar to a CES production function that has been widely estimated in the literature.

²⁷Equation (16) is again a semiparametric model with the additional restriction that the inverse function $h_H(\cdot)$ is of known form.

5 Labor-augmenting technological change

From equation (13) we obtain an estimate of the elasticity of substitution and recover labor-augmenting productivity at the firm level.

Elasticity of substitution. Tables 3 and 4 summarize different estimates of the elasticity of substitution. To facilitate the comparison with the existing literature, we proxy for $\tilde{\omega}_{Ljt}$ in equation (12) by a time trend $\tilde{\delta}_L t$ and estimate by OLS. As can be seen from columns (3) and (4) of Table 3, with the exception of industry 9, the estimates of the elasticity of substitution are in excess of one, whereas the estimates in the previous literature lie somewhere between 0 and 1 (Chirinko 2008, Bruno 1984, Rotemberg & Woodford 1996, Oberfield & Raval 2014). This reflects, first, that a time trend is a poor proxy for labor-augmenting technological change at the firm level and, second, that the estimates are upward biased as a result of the endogeneity problem. Nevertheless, the significant positive time trend once again previews the importance of labor-augmenting technological change.

We resolve the endogeneity problem by modeling the evolution of labor-augmenting productivity and estimating equation (13) by GMM. Columns (5)–(10) of Table 3 refer to the simplified model with $\lambda_1(S_{Tjt}) = 1$, $\lambda_2(S_{Tjt}) = 0$, and $\gamma_1(S_{Ojt}) = 0$. As expected the estimates of the elasticity of substitution are much lower and range from 0.45 to 0.64 as can be seen from column (5). With the exception of industries 6 and 8 in which σ is either implausibly high or low, we clearly reject the special cases of both a Leontieff ($\sigma \rightarrow 0$) and a Cobb-Douglas ($\sigma = 1$) production function.

Testing for overidentifying restrictions, we reject the validity of the moment conditions at a 5% level in five industries and we are close to rejecting in two more industries (columns (6) and (7)). To pinpoint the source of this problem, we exclude the subset of moments involving lagged materials m_{jt-1} from the estimation. As can be seen from columns (8)–(10), the estimates of the elasticity of substitution lie between 0.46 and 0.84 in all industries and at a 5% level we can no longer reject the validity of the moment conditions in any industry.

To see why the exogeneity of lagged materials m_{jt-1} is violated contrary to the timing of decisions in our model, recall that a firm engages in outsourcing if it can procure customized parts and pieces from its suppliers that are cheaper or better than what the firm can make in house from scratch. Lumping in-house and outsourced materials together pushes these quality differences into the error term. As outsourcing often relies on contractual relationships between the firm and its suppliers, the error term is likely correlated over time and thus with lagged materials m_{jt-1} as well.

The correction term $\gamma_1(S_{Ojt})$ in equation (13) absorbs quality differences between in-house and outsourced materials into the aggregator $\Gamma(M_{Ijt}, M_{Ojt})$ and accounts for the wedge that outsourcing may drive between the relative quantities and prices of materials and labor. The correction term $\lambda_2(S_{Tjt})$ similarly absorbs quality differences between permanent and temporary labor into the aggregator $\Lambda(L_{Pjt}, L_{Tjt})$ and accounts for adjustment costs

on permanent labor. As can be seen in columns (3)–(5) of Table 4, the correction terms duly restore the exogeneity of lagged materials m_{jt-1} as we cannot reject the validity of the moment conditions at a 5% level in any industry except for industry 7 in which we (barely) reject.²⁸ Our leading estimates of σ in column (3) of Table 4 lie between 0.44 and 0.80. Compared to the estimates in column (8) of Table 3, there are no systematic changes and our leading estimates are somewhat lower in five industries and somewhat higher in five industries. In sum, accounting for outsourcing and adjustment costs on permanent labor is an improvement over the assumption in Levinsohn & Petrin (2003) and many others that labor and materials are homogenous and static inputs and a key step in estimating the elasticity of substitution.

Our estimates of the elasticity of substitution are robust to purging the variation due to differences in the quality of labor from the lagged wage w_{jt-1} . In Appendix D, we use a wage regression to isolate the part of the wage that depends on the available data on the skill mix of a firm’s labor force. Using \widehat{w}_{Qjt-1} to denote this part, we replace w_{jt-1} as an instrument by $w_{jt-1} - \widehat{w}_{Qjt-1}$. Compared to column (3) of Table 4, the estimates of the elasticity of substitution in column (6) decrease somewhat in three industries, remain essentially unchanged in two industries, and increase somewhat in five industries.²⁹ The absence of substantial and systematic changes confirms that the variation in w_{jt-1} is exogenous with respect to $\widetilde{\xi}_{Ljt}$ and therefore useful in estimating equation (13).

Labor-augmenting technological change. With equation (13) estimated, we recover the labor-augmenting productivity $\omega_{Ljt} = \frac{\widetilde{\omega}_{Ljt}}{1-\sigma}$ of firm j in period t up to an additive constant from equation (10). We take the growth of labor-augmenting productivity at firm j in period t to be $\Delta\omega_{Ljt} = \omega_{Ljt} - \omega_{Ljt-1} \approx \frac{\exp(\omega_{Ljt}) - \exp(\omega_{Ljt-1})}{\exp(\omega_{Ljt-1})}$.³⁰ To obtain aggregate measures representing an industry, we account for the survey design by replicating the subsample of small firms $\frac{70\%}{5\%} = 14$ times before pooling it with the subsample of large firms. We report weighed averages of individual measures in Table 5, where the weight $\mu_{jt} = Y_{jt-2} / \sum_j Y_{jt-2}$ is the share of output of firm j in period $t - 2$.

In line with the patterns in the data described in Section 2, our estimates imply an important role for labor-augmenting technological change. As can be seen from column (1), labor-augmenting productivity grows quickly, on average, with rates of growth ranging

²⁸As noted in Section 3, we exclude observations with $S_{Tjt} = 0$ and thus $L_{Tjt} = 0$ because equation (7) presumes interior solutions for permanent and temporary labor. Compare columns (1) and (2) of Tables 1 and 3 with columns (1) and (2) of Table 4 for the exact number of observations and firms we exclude.

²⁹As we show in the Online Appendix, not much changes if we isolate the part of the wage that additionally depends on firm size to try and account for the quality of labor beyond our rather coarse data on the skill mix of a firm’s labor force (Oi & Idson 1999). Compared to column (3) of Table 4, the estimates of the elasticity of substitution decrease somewhat in three industries, remain essentially unchanged in three industries, and increase somewhat in four industries.

³⁰Given the specification of $\widetilde{g}_{L,t-1}(\widetilde{h}_L(\cdot), R_{jt-1})$ in equation (14), we exclude observations where a firm switches from performing to not performing R&D or vice versa between periods $t - 1$ and t from the subsequent analysis. We further exclude observations where a firm switches from zero to positive outsourcing or vice versa.

from 1.0% per year in industry 7 to 18.3% in industry 6 and above in industry 5. The rate of growth is, on average, slightly negative in industry 9. Hidden behind these averages is a tremendous amount of heterogeneity across firms. The rate of growth is positively correlated with the level of labor-augmenting productivity (column (2)), indicating that differences in labor-augmenting productivity between firms persist over time.

Ceteris paribus $\Delta\omega_{Ljt} \approx \frac{\exp(\omega_{Ljt})L_{jt}^* - \exp(\omega_{Ljt-1})L_{jt-1}^*}{\exp(\omega_{Ljt-1})L_{jt-1}^*}$ approximates the rate of growth of a firm's effective labor force $\exp(\omega_{Ljt-1})L_{jt-1}^*$. We approximate the rate of growth of the firm's output Y_{jt-1} by $\epsilon_{Ljt-2}\Delta\omega_{Ljt}$, where ϵ_{Ljt-2} is the elasticity of output with respect to the firm's effective labor force in period $t - 2$ (see Appendix C). This output effect, while close to zero in industry 9, ranges on average from 0.7% per year in industries 7 and 8 to 3.6% in industry 6, see column (3) of Table 5. Overall, labor-augmenting technological change causes output to grow in the vicinity of 2% per year.

Figure 1: Labor-augmenting technological change. Output effect. Index normalized to one in 1991.

Figure 1 illustrates the magnitude of labor-augmenting technological change and the heterogeneity in its impact across industries. The depicted index cumulates the year-to-year changes in labor-augmenting productivity in terms of output effects and is normalized to one in 1991.

Firms' R&D activities. While there is practically no difference in two industries, in eight industries firms that perform R&D have higher levels of labor-augmenting productivity than firms that do not perform R&D as can be seen from column (4) of Table 5. The rate of growth of labor-augmenting productivity for firms that perform R&D, on average, exceeds that of firms that do not perform R&D in eight industries. As can be seen from columns (5) and (6) of Table 5, the output effect for firms that perform R&D exceeds that of firms that do not perform R&D in six industries. Overall, our estimates indicate that firms' R&D activities are associated not only with higher levels of labor-augmenting productivity but by and large also with higher rates of growth of labor-augmenting productivity. Firms' R&D activities play a key role in determining the differences in labor-augmenting productivity across firms and the evolution of this component of productivity over time.

Skill upgrading. In our data, there is a shift from unskilled to skilled workers. For example, the share of engineers and technicians in the labor force increases from 7.2% in 1991 to 12.3% in 2006. While this shift has to be seen against the backdrop of a general increase of university graduates in Spain during the 1990s and 2000s, it begs the question how much skill upgrading contributes to the growth of labor-augmenting productivity.

To answer this question, we leverage our rather coarse data on the skill mix of a firm's labor force. Besides the share of temporary labor S_{Tjt} , our data has the share of white collar workers and the shares of engineers and technicians, respectively.³¹

We assume that there are Q types of permanent labor with qualities $1, \theta_2, \dots, \theta_Q$ and corresponding wages $W_{P1jt}, W_{P2jt}, \dots, W_{PQjt}$. The firm, facing this menu of qualities and wages, behaves as a price-taker in the labor market. In recognition of their different qualities, $L_{Pjt}^* = L_{P1jt} + \sum_{q=2}^Q \theta_q L_{Pqjt}$ is an aggregate of the Q types of permanent labor, with L_{Pqjt} being the quantity of permanent labor of type q at firm j in period t . $L_{jt}^* = \Lambda(L_{Pjt}^*, L_{Tjt})$ is the aggregate of permanent labor L_{Pjt}^* (instead of $L_{Pjt} = \sum_{q=1}^Q L_{Pqjt}$) and temporary labor L_{Tjt} in the production function in equation (1). Permanent labor is subject to convex adjustment costs $C_{BP}(B_{Pjt}, B_{Pjt-1})$, where $B_{Pjt} = \sum_{q=1}^Q W_{Pqjt} L_{Pqjt}$ is the wage bill for permanent labor. The state vector Ω_{jt} therefore includes $B_{Pjt-1}, W_{P1jt}, W_{P2jt}, \dots, W_{PQjt}$ instead of L_{Pjt-1} and W_{Pjt} .

The first-order condition for permanent labor of type q is

$$\nu \mu X_{jt}^{-\left(1 + \frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma} \omega_{Ljt}\right) (L_{jt}^*)^{-\frac{1}{\sigma}} \frac{\partial L_{jt}^*}{\partial L_{Pjt}^*} \theta_q = \frac{W_{Pqjt}(1 + \Delta_{jt})}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)}, \quad (18)$$

³¹We have these latter measures in the year a firm enters the sample and every subsequent four years. We take the skill mix to be unchanging in the interim.

where $\theta_1 = 1$ and the gap between the wage W_{Pqjt} and the shadow wage is

$$\begin{aligned}\Delta_{jt} &= \frac{\partial C_{B_P}(B_{Pjt}, B_{Pjt-1})}{\partial B_{Pjt}} - \frac{1}{W_{Pqjt}} \frac{1}{1+\rho} E_t \left[\frac{\partial V_{t+1}(\Omega_{jt+1})}{\partial L_{Pqjt}} | \Omega_{jt}, R_{jt} \right] \\ &= \frac{\partial C_{B_P}(B_{Pjt}, B_{Pjt-1})}{\partial B_{Pjt}} + \frac{1}{1+\rho} E_t \left[\frac{\partial C_{B_P}(B_{Pjt+1}, B_{Pjt})}{\partial B_{Pjt}} | \Omega_{jt}, R_{jt} \right].\end{aligned}$$

Equation (18) implies that $\theta_q = \frac{W_{Pqjt}}{W_{P1jt}}$ at an interior solution. While our data does not have $W_{P1jt}, W_{P2jt}, \dots, W_{PQjt}$, the wage regression in Appendix D enables us to recover θ_q by estimating the wage premium $\left(\frac{W_{Pqjt}}{W_{P1jt}} - 1 \right)$ of permanent labor of type q over type 1.

Multiplying equation (18) by the share S_{Pqjt} of permanent workers of type q and summing yields

$$\nu \mu X_{jt}^{-\left(1+\frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma} \omega_{Ljt}\right) (L_{jt}^*)^{-\frac{1}{\sigma}} \frac{\partial L_{jt}^*}{\partial L_{Pjt}^*} \Theta_{jt} = \frac{W_{Pjt}(1+\Delta_{jt})}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)}, \quad (19)$$

where $\Theta_{jt} = S_{P1jt} + \sum_{q=2}^Q \theta_q S_{Pqjt} = 1 + \sum_{q=2}^Q \left(\frac{W_{Pqjt}}{W_{P1jt}} - 1 \right) S_{Pqjt}$ is a quality index and $W_{Pjt} = \sum_{q=1}^Q W_{Pqjt} S_{Pqjt}$. Using Euler's theorem to combine equations (6) and (19) yields

$$\begin{aligned}&\nu \mu X_{jt}^{-\left(1+\frac{\nu\sigma}{1-\sigma}\right)} \exp(\omega_{Hjt}) \exp\left(-\frac{1-\sigma}{\sigma} \omega_{Ljt}\right) L_{jt}^{-\frac{1}{\sigma}} \Lambda((1-S_{Tjt})\Theta_{jt}, S_{Tjt})^{-\frac{1-\sigma}{\sigma}} \\ &= \frac{W_{jt} \left(1 + \frac{\Delta_{jt}}{1 + \frac{W_{Tjt} S_{Tjt}}{W_{Pjt} (1-S_{Tjt})}}\right)}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)} = \frac{W_{jt} \left(\frac{\Lambda_P((1-S_{Tjt})\Theta_{jt}, S_{Tjt})\Theta_{jt} + \frac{S_{Tjt}}{1-S_{Tjt}}}{\Lambda_T((1-S_{Tjt})\Theta_{jt}, S_{Tjt})} + \frac{S_{Tjt}}{W_{Tjt} + 1-S_{Tjt}}\right)}{P_{jt} \left(1 - \frac{1}{\eta(p_{jt}, D_{jt})}\right)}, \quad (20)\end{aligned}$$

where the second equality follows from dividing equations (6) and (19) and solving for Δ_{jt} . We proceed as before by assuming that $\frac{W_{Pjt}}{W_{Ljt}} = \lambda_0$ is an (unknown) constant and treating

$\frac{\Lambda_P((1-S_{Tjt})\Theta_{jt}, S_{Tjt})\Theta_{jt} + \frac{S_{Tjt}}{1-S_{Tjt}}}{\Lambda_T((1-S_{Tjt})\Theta_{jt}, S_{Tjt})} + \frac{S_{Tjt}}{W_{Tjt} + 1-S_{Tjt}} = \lambda_1(S_{Tjt}, \Theta_{jt})$ as an (unknown) function of S_{Tjt} and Θ_{jt} that

must be estimated nonparametrically. Replacing $\lambda_2(S_{Tjt}) = \ln\left(\lambda_1(S_{Tjt})\Lambda(1-S_{Tjt}, S_{Tjt})^{-\frac{1-\sigma}{\sigma}}\right)$

by $\lambda_2(S_{Tjt}, \Theta_{jt}) = \ln\left(\lambda_1(S_{Tjt}, \Theta_{jt})\Lambda((1-S_{Tjt})\Theta_{jt}, S_{Tjt})^{-\frac{1-\sigma}{\sigma}}\right)$ in our estimation equation (13) therefore accounts for types of permanent labor that differ in their qualities and wages.

The estimates of the elasticity of substitution in column (7) of Table 5 continue to hover around 0.6 across industries, with the exception of industries 4 and 8 in which they are implausibly low. Compared to column (3) of Table 4, they decrease somewhat in three industries, remain essentially unchanged in two industries, and increase somewhat in five industries. This further supports the notion that quality differences at a finer level than permanent and temporary labor are of secondary importance for estimating equation (13).

We develop the quality index Θ_{jt} mainly to “chip away at the productivity residual” by improving the measurement of inputs in the spirit of Caselli (2005) and the earlier produc-

tivity literature (Jorgenson 1995*a*, Jorgenson 1995*b*). As can be seen from column (10) of Table 5, skill upgrading indeed explains some, but by no means all of the growth of labor augmenting productivity. Compared to column (1), the rates of growth stay the same or go down in all industries. In industries 7, 8, 9, and 10 labor-augmenting productivity is stagnant or declining after accounting for skill upgrading, indicating that improvements in the skill mix over time are responsible for most of the growth of labor-augmenting productivity. In contrast, in industries 1, 2, 3, 4, 5, and 6, labor-augmenting productivity continues to grow after accounting for skill upgrading, albeit often at a much slower rate. In these industries, labor-augmenting productivity grows also because workers with a given set of skills become more productive over time.

6 Hicks-neutral technological change

From equation (13) we obtain an estimate of the elasticity of substitution and recover labor-augmenting productivity at the firm level. To recover Hicks-neutral productivity and the remaining parameters of the production function, we have to estimate equation (16).

Distributional parameters and elasticity of scale. Table 6 reports the distributional parameters β_K and $\beta_M = 1 - \beta_K$ and the elasticity of scale ν . Our estimates of β_K range from 0.07 in industry 8 to 0.31 in industry 6 (column (1)). Although the estimates of the elasticity of scale are rarely significantly different from one, taken together they suggest slightly decreasing returns to scale (columns (2)). We cannot reject the validity of the moment conditions in any industry by a wide margin (columns (3) and (4)).

Hicks-neutral technological change. With equation (16) estimated, we recover Hicks-neutral productivity ω_{Hjt} up to an additive constant from equation (11). We take the growth of Hicks-neutral productivity at firm j in period t to be $\Delta\omega_{Hjt} = \omega_{Hjt} - \omega_{Hjt-1} \approx \frac{\exp(\omega_{Hjt}) - \exp(\omega_{Hjt-1})}{\exp(\omega_{Hjt-1})}$. Ceteris paribus $\Delta\omega_{Hjt} \approx \frac{X_{jt-1}^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt}) \exp(e_{jt-1}) - X_{jt-1}^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt-1}) \exp(e_{jt-1})}{X_{jt-1}^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt-1}) \exp(e_{jt-1})}$ approximates the rate of growth of a firm's output Y_{jt-1} . The rate of growth of Hicks-neutral productivity is therefore directly comparable to the output effect of labor-augmenting technological change. We proceed as before to obtain aggregate measures representing an industry.

As can be seen from column (1) of Table 7, Hicks-neutral productivity grows quickly in five industries, with rates of growth ranging, on average, from 1.2% per year in industry 8 to 4.4% in industry 1. It grows much more slowly or barely at all in three industries, with rates of growth below 0.5% per year. While there is considerable heterogeneity in the rate of growth of Hicks-neutral productivity across industries, overall Hicks-neutral technological change causes output to grow in the vicinity of 2% per year. Once again, the rate of growth

is positively correlated with the level of Hicks-neutral productivity (column (2)), indicating that differences in Hicks-neutral productivity between firms persist over time.

Figure 2: Hicks-neutral technological change. Index normalized to one in 1991.

Figure 2 illustrates the magnitude of Hicks-neutral technological change. The depicted index cumulates the year-to-year changes in Hicks-neutral productivity and is normalized to one in 1991.³² The heterogeneity in the impact of Hicks-neutral technological change across industries clearly exceeds that of labor-augmenting technological change (see again Figure 1).

Taken together labor-augmenting and Hicks-neutral technological change cause output to grow by, on average, between 0.7% in industry 7 and 7.8% in industry 6, as can be seen in column (3) of Table 7. The components of productivity are positively correlated. This correlation is slightly stronger in the rates of growth (column (4)) as it is in levels.

Firms' R&D activities. As can be seen from column (5) of Table 7, firms that perform R&D have higher levels of Hicks-neutral productivity than firms that do not perform R&D in six industries but lower levels of Hicks-neutral productivity in four industries. While there is practically no difference in industry 10, the rate of growth of Hicks-neutral productivity for firms that perform R&D, on average, exceeds that of firms that do not perform R&D

³²In industry 9, in line with column (1) of Table 7, we trim values of $\Delta\omega_H$ below -0.25 and above 0.5 .

in five industries, as can be seen from columns (6) and (7). Overall, our estimates indicate that firms' R&D activities are associated with higher levels and rates of growth of Hicks-neutral productivity, although firms' R&D activities seem less closely tied to Hicks-neutral than to labor-augmenting productivity. This is broadly consistent with the large literature on induced innovation that argues that firms direct their R&D activities to conserve the relatively more expensive factors of production, in particular labor.³³

7 Capital-augmenting technological change

As discussed in Section 2, the evolution of the relative quantities and prices of the various factors of production provides no evidence for capital-augmenting technological change. Our leading specification therefore restricts the productivities of capital and materials to change at the same rate and in lockstep with Hicks-neutral technological change. A more general specification allows for capital-augmenting productivity ω_{Kjt} so that equation (1) (with $\beta_0 = \beta_L = 1$) becomes

$$Y_{jt} = \left[\beta_K (\exp(\omega_{Kjt})K_{jt})^{-\frac{1-\sigma}{\sigma}} + (\exp(\omega_{Ljt})L_{jt}^*)^{-\frac{1-\sigma}{\sigma}} + \beta_M (M_{jt}^*)^{-\frac{1-\sigma}{\sigma}} \right]^{-\frac{\nu\sigma}{1-\sigma}} \exp(\omega_{Hjt}) \exp(e_{jt}). \quad (21)$$

We explore the role of capital-augmenting technological change in our data in two ways.

First, we follow Raval (2013) and parts of the previous literature on estimating aggregate production functions (see Antràs (2004) and the references therein) and assume that capital is a static input that is chosen each period to maximize short-run profits. In analogy to equation (10), we recover (conveniently rescaled) capital-augmenting productivity $\tilde{\omega}_{Kjt} = (1 - \sigma)\omega_{Kjt}$ as

$$\begin{aligned} \tilde{\omega}_{Kjt} &= \tilde{\gamma}_K + m_{jt} - k_{jt} + \sigma(p_{Mjt} - p_{Kjt}) + (1 - \sigma)\gamma_1(S_{Ojt}) \\ &\equiv \tilde{h}_K(m_{jt} - k_{jt}, p_{Mjt} - p_{Kjt}, S_{Ojt}), \end{aligned} \quad (22)$$

where $\tilde{\gamma}_K = -\sigma \ln\left(\frac{\beta_M}{\beta_K}\right)$ and we use the user cost of capital in our data as a rough measure of the price of capital p_{Kjt} . Using our leading estimates from Section 5, we recover the capital-augmenting productivity $\omega_{Kjt} = \frac{\tilde{\omega}_{Kjt}}{1-\sigma}$ of firm j in period t .³⁴ $\Delta\omega_{Kjt}$ in column (1) of Table 8 approximates the rate of growth of a firm's effective capital stock $\exp(\omega_{Kjt-1})K_{jt-1}$ and

³³More explicitly testing for induced innovation is difficult because we do not observe what a firm does with its R&D expenditures. One way to proceed may be to add interactions of R&D expenditures and input prices to the laws of motion in equations (2) and (3). We leave this to future research.

³⁴As an alternative to plugging our leading estimates from Section 5 into equation (22), in the Online Appendix we use equation (22) to form the analog to our first estimation equation (13):

$$\begin{aligned} m_{jt} - k_{jt} &= -\sigma(p_{Mjt} - p_{Kjt}) - (1 - \sigma)\gamma_1(S_{Ojt}) \\ &+ \tilde{g}_{Kt-1}(\tilde{h}_K(m_{jt-1} - k_{jt-1}, p_{Mjt-1} - p_{Kjt-1}, S_{Ojt-1}), R_{jt-1}) + \tilde{\xi}_{Kjt}. \end{aligned}$$

Consistent with measurement error in p_{Kjt} , the resulting estimates of σ are very noisy and severely biased toward zero.

$\epsilon_{Kjt-2}\Delta\omega_{Kjt}$ in column (2) the rate of growth of the firm's output Y_{jt-1} , where ϵ_{Kjt-2} is the elasticity of output with respect to the firm's effective capital stock (see Appendix C). As can be seen from column (1), capital-augmenting productivity grows slowly, on average, with rates of growth of 0.8% per year in industry 6, 2.2% in industry 10, and 5.6% in industry 1. The rate of growth is negative in the remaining seven industries. The growth of capital-augmenting productivity is especially underwhelming in comparison to the growth of labor-augmenting productivity (see again column (1) of Table 5). The output effect in column (2) is also close to zero in all industries, although this likely reflects the fact that capital is not a static input. As the user cost of capital excludes adjustment costs, it falls short of the shadow price of capital, and using it drives down the elasticity of output with respect to the firm's effective capital stock.

Second, we return to the usual setting in the literature following Olley & Pakes (1996) and allow the choice of capital to have dynamic implications. We follow parts of the previous literature on estimating aggregate production functions and proxy for ω_{Kjt} by a time trend $\delta_K t$. Our second estimation equation (16) remains unchanged except that

$$X_{jt} = \beta_K (\exp(\delta_K t) K_{jt})^{-\frac{1-\sigma}{\sigma}} + \beta_M (M_{jt} \exp(\gamma_1(S_{Ojt})))^{-\frac{1-\sigma}{\sigma}} \left(\frac{1 - S_{Mjt}}{S_{Mjt}} \lambda_1(S_{Tjt}) + 1 \right).$$

Columns (3)–(7) of Table 8 summarize the resulting estimates of β_K , ν , and δ_K . The estimates of β_K and ν are very comparable to those in Table 5. Moreover, the insignificant time trend leaves little room for capital-augmenting technological change in our data.

In sum, in line with the patterns in the data described in Section 2, there is little, if any, evidence for capital-augmenting technological change in our data. Of course, our ways of exploring the role of capital-augmenting technological change are less than ideal in that they either rest on the assumption that capital is a static input or abstract from firm-level heterogeneity in capital-augmenting productivity. An important question is therefore whether our approach can be extended to treat capital-augmenting productivity on par with labor-augmenting and Hicks-neutral productivity. Recovering a third component of productivity, at a bare minimum, requires a third decision to invert besides labor and materials. Investment is a natural candidate. Unlike the demand for labor and materials, however, investment depends on the details of the firm's dynamic programming problem. Hence, it may have to be inverted nonparametrically as in Olley & Pakes (1996). There are two principal difficulties. First, one has to prove that the observed demands for labor and materials along with investment are jointly invertible for unobserved capital-augmenting, labor-augmenting, and Hicks-neutral productivity. This is not an easy task given the difficulties Buettner (2005) encountered in a much simpler dynamic programming problem. Second, the inverse functions $\tilde{h}_K(\cdot)$, $\tilde{h}_L(\cdot)$, and $h_H(\cdot)$ are high-dimensional. Thus, estimating these functions nonparametrically is demanding on the data.

Related literature. As mentioned in Section 1, our paper is related to Grieco et al. (2015) and subsequent work in progress by Zhang (2014*a*, 2014*b*). These papers build on Doraszelski & Jaumandreu (2013) by exploiting the parameter restrictions between the production function and input demand functions to infer unobservables from observables. Because their data contains the materials bill rather than its split into price and quantity, Grieco et al. (2015) assume that labor and materials are both static inputs that are chosen each period to maximize short-run profits and solve the implied first-order conditions for the firm’s Hicks-neutral productivity and the price of materials that the firm faces. Zhang (2014*a*, 2014*b*) proxies for the price of materials by a regional price index (similar to Raval 2013) and instead solves the first-order conditions for the firm’s capital- and labor-augmenting productivity. One difference to our approach is that Grieco et al. (2015) and Zhang (2014*a*, 2014*b*) plug the recovered unobservables back into the production function. While this avoids assumptions on the law of motion for productivity, parameters of interest may cancel depending on the specification of the production function (see Example 3.1 of Grieco et al. (2015) and Section 4 of Akerberg et al. (2006)).

Using firm-level panel data for the Chinese steel industry, Zhang (2014*b*) adds Hicks-neutral productivity to the model in Zhang (2014*a*) and specifies an uncontrolled first-order, time-homogenous Markov process for it. He infers this additional unobservable from investment (though without proving invertibility). The empirical strategy draws on Akerberg et al. (2006) in that Hicks-neutral productivity ω_{Hjt} is separated from the random shock e_{jt} in a first nonparametric step (though without accounting for prices and correcting for the endogeneity of the revenue shares of labor and materials with respect to the random shock). In a second step, the parameters of the production function are estimated off the law of motion for ω_{Hjt} . By comparing the means and standard deviations of ω_{Kjt} , ω_{Ljt} , and ω_{Hjt} , Zhang (2014*b*) concludes that firm-level heterogeneity is largest in labor-augmenting productivity (though this conclusion can be questioned by recalling that ω_{Kjt} , ω_{Ljt} , and ω_{Hjt} can only be recovered up to additive constants and are measured in non-comparable units anyway).

8 Conclusions

Technological change can increase the productivity of capital, labor, and the other factors of production in equal terms or it can be biased towards a specific factor. In this paper, we directly assess the bias of technological change by measuring, at the level of the individual firm, how much of technological change is labor augmenting and how much of it is Hicks neutral.

To this end, we develop a dynamic model of the firm in which productivity is multi-dimensional. At the center of the model is a CES production function that parsimoniously relates the relative quantities of materials and labor to their relative prices and labor-

augmenting productivity. To properly isolate and measure labor-augmenting productivity, we account for other factors that impact this relationship, in particular, outsourcing and adjustment costs on permanent labor.

We apply our estimator to an unbalanced panel of 2375 Spanish manufacturing firms in ten industries from 1990 to 2006. Our estimates indicate limited substitutability between the various factors of production. This calls into question whether the widely-used Cobb-Douglas production function with its unitary elasticity of substitution adequately represents firm-level production processes.

Our estimates provide clear evidence that technological change is biased. *Ceteris paribus* labor-augmenting technological change causes output to grow, on average, in the vicinity of 2% per year. While skill upgrading explains some of the growth of labor augmenting productivity, in many industries labor-augmenting productivity grows because workers with a given set of skills become more productive over time. In short, our estimates cast doubt on the assumption of Hicks-neutral technological change that underlies many of the standard techniques for measuring productivity and estimating production functions.

At the same time, our estimates do not validate the assumption that technological change is purely labor augmenting that plays a central role in the literature on economic growth. In addition to labor-augmenting technological change, our estimates show that Hicks-neutral technological change causes output to grow, on average, in the vicinity of 2% per year.

Behind these averages lies a substantial amount of heterogeneity across industries and firms. Our estimates point to substantial and persistent differences in labor-augmenting and Hicks-neutral productivity between firms. Firms' R&D activities play a key role in determining these differences and their evolution over time. Interestingly, our estimates indicate that labor-augmenting productivity is slightly more closely tied to firms' R&D activities than to Hicks-neutral productivity. Through the lens of the literature on induced innovation this may be viewed as supporting the argument that firms direct their R&D activities to conserve on labor.

An interesting avenue for future research is to investigate the implications of the different types of technological change for employment. Recent research points to biased technological change as a key driver of the diverging experiences of the continental European, U.S., and U.K. economies during the 1980s and 1990s (Blanchard 1997, Caballero & Hammour 1998, Bentolila & Saint-Paul 2004, McAdam & Willman 2013). Our estimates lend themselves to decomposing firm-level changes in employment into displacement, substitution, and output effects and to compare these effects between labor-augmenting and Hicks-neutral technological change. This may be helpful for better understanding and predicting the evolution of employment as well as for designing labor market and innovation policies in the presence of biased technological change.

Appendix A Data

We observe firms for a maximum of 17 years between 1990 and 2006. We restrict the sample to firms with at least three years of data on all variables required for estimation. The number of firms with 3, 4, ..., 17 years of data is 313, 240, 218, 215, 207, 171, 116, 189, 130, 89, 104, 57, 72, 94, and 160, respectively. Table A1 gives the industry definitions along with their equivalent definitions in terms of the ESEE, National Accounts, and ISIC classifications (columns (1)–(3)). Based on the National Accounts in 2000, we further report the shares of the various industries in the total value added of the manufacturing sector (column (4)).

In what follows we define the variables we use. We begin with the variables that are relevant for our main analysis.

- *Investment.* Value of current investments in equipment goods (excluding buildings, land, and financial assets) deflated by the price index of investment. The price of investment is the equipment goods component of the index of industry prices computed and published by the Spanish Ministry of Industry. By measuring investment in operative capital we avoid some of the more severe measurement issues of the other assets.
- *Capital.* Capital at current replacement values \tilde{K}_{jt} is computed recursively from an initial estimate and the data on current investments in equipment goods \tilde{I}_{jt} . We update the value of the past stock of capital by means of the price index of investment P_{It} as $\tilde{K}_{jt} = (1 - \delta) \frac{P_{It}}{P_{It-1}} \tilde{K}_{jt-1} + \tilde{I}_{jt-1}$, where δ is an industry-specific estimate of the rate of depreciation. Capital in real terms is obtained by deflating capital at current replacement values by the price index of investment as $K_{jt} = \frac{\tilde{K}_{jt}}{P_{It}}$.
- *Labor.* Total hours worked computed as the number of workers times the average hours per worker, where the latter is computed as normal hours plus average overtime minus average working time lost at the workplace.
- *Materials.* Value of intermediate goods consumption (including raw materials, components, energy, and services) deflated by a firm-specific price index of materials.
- *Output.* Value of produced goods and services computed as sales plus the variation of inventories deflated by a firm-specific price index of output.
- *Wage.* Hourly wage cost computed as total labor cost including social security payments divided by total hours worked.
- *Price of materials.* Firm-specific price index for intermediate consumption. Firms are asked about the price changes that occurred during the year for raw materials, components, energy, and services. The price index is computed as a Paasche-type index of the responses.
- *Price of output.* Firm-specific price index for output. Firms are asked about the price changes they made during the year in up to 5 separate markets in which they operate. The price index is computed as a Paasche-type index of the responses.
- *Demand shifter.* Firms are asked to assess the current and future situation of the main market in which they operate. The demand shifter codes the responses as 0, 0.5, and 1 for slump, stability, and expansion, respectively.

- *Share of temporary labor.* Fraction of workers with fixed-term contracts and no or small severance pay.
- *Share of outsourcing.* Fraction of customized parts and pieces that are manufactured by other firms in the value of the firm’s intermediate goods purchases.
- *R&D expenditures.* R&D expenditures include the cost of intramural R&D activities, payments for outside R&D contracts with laboratories and research centers, and payments for imported technology in the form of patent licensing or technical assistance, with the various expenditures defined according to the OECD Oslo and Frascati manuals.

We next turn to additional variables that we use for descriptive purposes, extensions, and robustness checks.

- *User cost of capital.* Computed as $P_{It}(r_{jt} + \delta - CPI_t)$, where P_{It} is the price index of investment, r_{jt} is a firm-specific interest rate, δ is an industry-specific estimate of the rate of depreciation, and CPI_t is the rate of inflation as measured by the consumer price index.
- *Skill mix.* Fraction of non-production employees (white collar workers), workers with an engineering degree (engineers), and workers with an intermediate degree (technicians).
- *Region.* Dummy variables corresponding to the 19 Spanish autonomous communities and cities where employment is located if it is located in a unique region and another dummy variable indicating that employment is spread over several regions.
- *Product submarket.* Dummy variables corresponding to a finer breakdown of the 10 industries into subindustries (restricted to subindustries with at least 5 firms, see column (5) of Table A1).
- *Technological sophistication.* Dummy variable that takes the value one if the firm uses digitally controlled machines, robots, CAD/CAM, or some combination of these procedures.
- *Identification between ownership and control.* Dummy variable that takes the value one if the owner of the firm or the family of the owner hold management positions.
- *Age.* Years elapsed since the foundation of the firm with a maximum of 40 years.
- *Firm size.* Number of workers in the year the firm enters the sample.

Appendix B Estimation

Unknown functions. The functions $\tilde{g}_{L1}(\tilde{h}_L(\cdot))$, $\tilde{g}_{L2}(\tilde{h}_L(\cdot), r_{jt-1})$, $g_{H1}(h_H(\cdot))$, and $g_{H2}(h_H(\cdot), r_{jt-1})$ that are part of the conditional expectation functions $\tilde{g}_{Lt-1}(\tilde{h}_L(\cdot), R_{jt-1})$ and $g_{Ht-1}(h_H(\cdot), R_{jt-1})$ are unknown and must be estimated nonparametrically, as must be the absolute value of the price elasticity $\eta(p_{jt}, D_{jt})$ and the correction terms $\lambda_1(S_{Tjt})$, $\lambda_2(S_{Tjt})$, and $\gamma_1(S_{Ojt})$. Following Wooldridge (2004), we model an unknown function $q(v)$ of one variable v by a univariate polynomial of degree Q . We model an unknown function $q(u, v)$ of two variables

u and v by a complete set of polynomials of degree Q (see Judd 1998). Unless otherwise noted, we omit the constant in $q(\cdot)$ and set $Q = 3$ in the remainder of this paper.

Starting with the conditional expectation functions, we specify $\tilde{g}_{L1}(\tilde{h}_L(\cdot)) = q(\tilde{h}_L(\cdot) - \tilde{\gamma}_L)$, $\tilde{g}_{L2}(\tilde{h}_L(\cdot), r_{jt}) = q_0 + q(\tilde{h}_L(\cdot) - \tilde{\gamma}_L, r_{jt})$, $g_{H1}(h_H(\cdot)) = q(h_H(\cdot) - \gamma_H)$, and $g_{H2}(h_H(\cdot), r_{jt}) = q_0 + q(h_H(\cdot) - \gamma_H, r_{jt})$, where q_0 is a constant and the function $q(\cdot)$ is modeled as described above. Without loss of generality, we absorb $\tilde{\gamma}_L$ and γ_H into the overall constants of our estimation equations. Turning to the absolute value of the price elasticity, to impose the theoretical restriction $\eta(p_{jt}, D_{jt}) > 1$, we specify $\eta(p_{jt}, D_{jt}) = 1 + \exp(q(p_{jt}, D_{jt}))$, where the function $q(\cdot)$ is modeled as described above except that we suppress terms involving D_{jt}^2 and D_{jt}^3 . Turning to the correction terms, we specify $\lambda_1(S_{Tjt}) = q(\ln S_{Tjt})$ and $\lambda_2(S_{Tjt}) = q(\ln S_{Tjt})$ in industries 2, 3, and 10 and $\lambda_1(S_{Tjt}) = q(\ln(1 - S_{Tjt}))$ and $\lambda_2(S_{Tjt}) = q(\ln(1 - S_{Tjt}))$ in the remaining industries.³⁵ Finally, we specify $\gamma_1(S_{Ojt}) = q(S_{Ojt})$; this ensures that $\gamma_1(S_{Ojt}) = 0$ if $S_{Ojt} = 0$ in line with the normalization $\Gamma(M_{Ijt}, 0) = M_{Ijt}$.

Parameters and instruments. Our first estimation equation (13) has 36 parameters: constant, σ , 15 parameters in $\tilde{g}_{L0}(t - 1)$ (time dummies), 3 parameters in $\tilde{g}_{L1}(\tilde{h}_L(\cdot))$, 10 parameters in $\tilde{g}_{L2}(\tilde{h}_L(\cdot), r_{jt-1})$, 3 parameters in $\lambda_2(S_{Tjt})$, and 3 parameters in $\gamma_1(S_{Ojt})$.

Our instrumenting strategy is adapted from Doraszelski & Jaumandreu (2013) and we refer the reader to Doraszelski & Jaumandreu (2013) and the references therein for a discussion of the use of polynomials for instruments. We use the constant, 15 time dummies, the dummy for performers $1(R_{jt-1} > 0)$, the demand shifter D_{jt} , and a univariate polynomial in $\ln S_{Ojt-1} + m_{jt-1}$ interacted with $1(S_{Ojt-1} > 0)$ (3 instruments). We further use a complete set of polynomials in l_{jt-1} , m_{jt-1} , and $p_{Mjt-1} - w_{jt-1}$ interacted with the dummy for nonperformers $1(R_{jt-1} = 0)$ (19 instruments). In industries 5 and 8 we replace $p_{Mjt-1} - w_{jt-1}$ by p_{Mjt-1} in the complete set of polynomials. Finally, we use a complete set of polynomials in l_{jt-1} , m_{jt-1} , and $p_{Mjt-1} - w_{jt-1}$ and r_{jt-1} interacted with the dummy for performers $1(R_{jt-1} > 0)$ (34 instruments). This yields a total of 74 instruments and $74 - 36 = 38$ degrees of freedom (see column (4) of Table 4).

After imposing the estimated values from equation (13), our second estimation equation (16) has 40 parameters: constant, β_K , ν , 15 parameters in $g_{H0}(t - 1)$ (time dummies), 3 parameters in $g_{H1}(h_H(\cdot))$, 10 parameters in $g_{H2}(h_H(\cdot), r_{jt-1})$, 3 parameters in $\lambda_1(S_{Tjt})$, and 6 parameters in $\eta(p_{jt}, D_{jt})$.

As before, we use polynomials for instruments. We use the constant, 15 time dummies, the dummy for performers $1(R_{jt-1} > 0)$, the demand shifter D_{jt} , a univariate polynomial in p_{jt-1} (3 instruments), a univariate polynomial in $p_{Mjt-1} - p_{jt-1}$ (3 instruments), and a univariate polynomial in k_{jt} (3 instruments). We also use a complete set of polynomials in $M_{jt-1} \frac{1 - S_{Mjt-1}}{S_{Mjt-1}}$ and K_{jt-1} interacted with the dummy for nonperformers $1(R_{jt-1} = 0)$ (9 instruments). Finally, we use a complete set of polynomials in $M_{jt-1} \frac{1 - S_{Mjt-1}}{S_{Mjt-1}}$ and K_{jt-1} (9 instruments) and a univariate polynomial in r_{jt-1} interacted with the dummy for performers $1(R_{jt-1} > 0)$ (3 instruments). This yields a total of 48 instruments and $48 - 40 = 8$ degrees of freedom in industries 1, 2, 3, 6, 7, 9, and 10 (see column (3) of Table 6). In industries 4, 5, and 8, we add a univariate polynomial in $\ln(1 - S_{Tjt-1})$ (3 instruments). We replace the univariate polynomial in k_{jt} by k_{jt} in industries 4 and 8 and we drop D_{jt} in industry 5.

³⁵To incorporate skill upgrading, we instead specify $\lambda_1(S_{Tjt}, \Theta_{jt}) = q(\ln S_{Tjt}, \ln \Theta_{jt})$ and $\lambda_2(S_{Tjt}, \Theta_{jt}) = q(\ln S_{Tjt}, \ln \Theta_{jt})$ in industries 2, 3, and 10 and $\lambda_1(S_{Tjt}, \Theta_{jt}) = q(\ln(1 - S_{Tjt}), \ln \Theta_{jt})$ and $\lambda_2(S_{Tjt}, \Theta_{jt}) = q(\ln(1 - S_{Tjt}), \ln \Theta_{jt})$ in the remaining industries, where the function $q(\cdot)$ is modeled as described above except that we suppress terms involving $(\ln \Theta_{jt})^2$ and $(\ln \Theta_{jt})^3$.

Estimation. From the GMM problem in equation (17) with weighting matrix $\widehat{W}_L = \left[\frac{1}{N} \sum_j A_{Lj}(z_j) A_{Lj}(z_j)' \right]^{-1}$ we first obtain a consistent estimate $\widehat{\theta}_L$ of θ_L . This first step is the NL2SLS estimator of Amemiya (1974). In the second step, we compute the optimal estimate with weighting matrix $\widehat{W}_L = \left[\frac{1}{N} \sum_j A_{Lj}(z_j) \nu_{Lj}(\widehat{\theta}_L) \nu_{Lj}(\widehat{\theta}_L)' A_{Lj}(z_j)' \right]^{-1}$. Throughout the paper, we report standard errors that are robust to heteroskedasticity and autocorrelation.

Implementation. Gauss code for our estimator is available from the authors upon request along with instructions for obtaining the data. To reduce the number of parameters to search over in the GMM problem in equation (17), we “concentrate out” the parameters that enter it linearly (Wooldridge 2010, p. 435). To guard against local minima, we have extensively searched over the remaining parameters, often using preliminary estimates to narrow down the range of these parameters.

Testing. The value of the GMM objective function for the optimal estimator, multiplied by N , has a limiting χ^2 distribution with $Q - P$ degrees of freedom, where Q is the number of instruments and P the number of parameters to be estimated. We use it as a test for overidentifying restrictions or validity of the moment conditions.

Appendix C Output effect

Direct calculation starting from equation (1) yields the elasticity of output with respect to a firm’s effective labor force:

$$\begin{aligned} \epsilon_{Ljt} &= \frac{\partial Y_{jt}}{\partial \exp(\omega_{Ljt}) L_{jt}^*} \frac{\exp(\omega_{Ljt}) L_{jt}^*}{Y_{jt}} \\ &= \frac{\nu \left(\exp(\omega_{Ljt}) L_{jt}^* \right)^{-\frac{1-\sigma}{\sigma}}}{\beta_K K_{jt}^{-\frac{1-\sigma}{\sigma}} + \left(\exp(\omega_{Ljt}) L_{jt}^* \right)^{-\frac{1-\sigma}{\sigma}} + \beta_M \left(M_{jt}^* \right)^{-\frac{1-\sigma}{\sigma}}}. \end{aligned}$$

Using equation (10) to substitute for ω_{Ljt} and simplifying we obtain

$$\epsilon_{Ljt} = \frac{\nu^{\frac{1-S_{Mjt}}{S_{Mjt}}} \lambda_1(S_{Tjt})}{\frac{\beta_K}{\beta_M} \left(\frac{K_{jt}}{M_{jt} \exp(\gamma_1(S_{Ojt}))} \right)^{-\frac{1-\sigma}{\sigma}} + \frac{1-S_{Mjt}}{S_{Mjt}} \lambda_1(S_{Tjt}) + 1}. \quad (23)$$

Recall from equation (7) that $\lambda_1(S_{Tjt}) = 1 + \frac{\Delta_{jt}}{1 + \frac{W_{Tjt}}{W_{Pjt}} \frac{S_{Tjt}}{1-S_{Tjt}}}$, where Δ_{jt} is the gap between the wage of permanent workers W_{Pjt} and the shadow wage. To facilitate evaluating equation (23), we abstract from adjustment costs and set $\lambda_1(S_{Tjt}) = 1$.

Direct calculation starting from equation (21) also yields the elasticity of output with

respect to a firm's effective capital stock:

$$\begin{aligned}
\epsilon_{Kjt} &= \frac{\partial Y_{jt}}{\partial \exp(\omega_{Kjt})K_{jt}} \frac{\exp(\omega_{Kjt})K_{jt}}{Y_{jt}} \\
&= \frac{\nu (\exp(\omega_{Kjt})K_{jt})^{-\frac{1-\sigma}{\sigma}}}{(\exp(\omega_{Kjt})K_{jt})^{-\frac{1-\sigma}{\sigma}} + \left(\exp(\omega_{Ljt})L_{jt}^*\right)^{-\frac{1-\sigma}{\sigma}} + \beta_M \left(M_{jt}^*\right)^{-\frac{1-\sigma}{\sigma}}} \\
&= \frac{\nu}{1 + \frac{P_{Mjt}M_{jt}}{P_{Kjt}K_{jt}} \left(\frac{1-S_{Mjt}}{S_{Mjt}} \lambda_1(S_{Tjt}) + 1\right)}, \tag{24}
\end{aligned}$$

where we use equations (10) and (22) to substitute for ω_{Ljt} and ω_{Kjt} , respectively. As with equation (23), we set $\lambda_1(S_{Tjt}) = 1$ to evaluate equation (24).

Appendix D Wage regression

As column (1) of Table A2 shows, the coefficient of variation for the (level of the) wage W_{jt} ranges from 0.35 to 0.50 across industries.³⁶ The variance decomposition in columns (2)–(4) shows that around one quarter of the overall variation is within firms across periods. The larger part of this variation is across firms.

To explore the source of this variation, we regress the (log of the) wage w_{jt} on the skill mix of a firm's labor force as given by the share of temporary (as opposed to permanent) labor, the share of white (as opposed to blue) collar workers, and the shares of engineers and technicians (as opposed to unskilled workers), time dummies, region dummies, product submarket dummies, the demand shifter, and an array of other firm characteristics, namely dummies for technological sophistication and identification of ownership and control as well as univariate polynomials of degree 3 in age and firm size.

To motivate this regression, assume that there are Q types of labor with wages W_{1jt} , W_{2jt}, \dots, W_{Qjt} and write the wage as

$$W_{jt} = \sum_{q=1}^Q W_{qjt} S_{qjt} = W_{1jt} \left(1 + \sum_{q=2}^Q \left(\frac{W_{qjt}}{W_{1jt}} - 1 \right) S_{qjt} \right),$$

where S_{qjt} is the share of labor of type q and $\sum_{q=1}^Q S_{qjt} = 1$. Because

$$w_{jt} \approx w_{1jt} + \sum_{q=2}^Q \left(\frac{W_{qjt}}{W_{1jt}} - 1 \right) S_{qjt},$$

the coefficient on S_{qjt} in the wage regression is an estimate of the wage premium $\left(\frac{W_{qjt}}{W_{1jt}} - 1 \right)$ of labor of type q over type 1. Because we do not have the joint distribution of skills (e.g., temporary white collar technician) in our data, we approximate it by the marginal distributions (e.g., share of temporary labor) and ignore higher-order terms. As columns (5)–(8) of Table A2 show, the estimated coefficients on the skill mix of a firm's labor force are often significant, have the expected signs, and are quite similar across industries. On average across industries, temporary workers earn 36% less than permanent workers, white

³⁶The coefficient of variation for the price of materials ranges from 0.12 to 0.19 across industries.

collar workers earn 26% more than blue collar workers, engineers earn 85% more than unskilled workers, and technicians earn 23% more than unskilled workers.

The wage regression also shows that some, but by no means all variation in the wage is due to worker quality. To isolate the part of the wage that depends on the skill mix of a firm's labor force, we decompose the predicted wage \widehat{w}_{jt} into a prediction \widehat{w}_{Qjt} based on the skill mix and a prediction \widehat{w}_{Cjt} based on the remaining variables. \widehat{w}_{Qjt} and \widehat{w}_{Cjt} are positively correlated. According to $R^2 = \frac{Var(\widehat{w}_{jt})}{Var(w_{jt})}$ in column (9), depending on the industry, the wage regression explains between 63% and 76% of the variation in the wage, with an average of 70%. The skill mix by itself explains between 2% and 20% of the variation in the wage, with an average of 10% (see $R_Q^2 = \frac{Var(\widehat{w}_{Qjt})}{Var(w_{jt})}$ in column (10)). In contrast, the remaining variables explain between 36% and 64% of the variation in the wage, with an average of 48% (see $R_C^2 = \frac{Var(\widehat{w}_{Cjt})}{Var(w_{jt})}$ in column (11)). The larger part of the variation in the wage therefore appears to be due to temporal and geographic differences in the supply of labor, the fact that firms operate in different product submarkets, and other firm characteristics.

In developing the quality index Θ_{jt} , we assume that there are Q types of permanent labor. We approximate the wage premium $\left(\frac{W_{Pqjt}}{W_{P1jt}} - 1\right)$ of permanent labor of type q over type 1 by the estimated coefficient on S_{qjt} in the wage regression and the share $S_{Pqjt} = \frac{L_{Pqjt}}{L_{Pjt}} = \frac{L_{Pqjt}}{L_{jt}} \Big/ \frac{L_{Pjt}}{L_{jt}}$ of permanent labor of type q by $\frac{S_{qjt}}{1-S_{Tjt}}$.

References

- Abowd, J., Haltiwanger, J., Lane, J., McKinney, K. & Sandusky, K. (2007), Technology and the demand for skill: An analysis of within and between firm differences, Working paper no. 13043, NBER, Cambridge.
- Acemoglu, D. (2002), 'Directed technical change', *Review of Economic Studies* **69**, 781–809.
- Acemoglu, D. (2003), 'Labor- and capital-augmenting technical change', *Journal of the European Economic Association* **1**(1), 1–37.
- Ackerberg, D., Benkard, L., Berry, S. & Pakes, A. (2007), Econometric tools for analyzing market outcomes, in J. Heckman & E. Leamer, eds, 'Handbook of Econometrics', Vol. 6A, North-Holland, Amsterdam, pp. 4171–4276.
- Ackerberg, D., Caves, K. & Frazer, G. (2006), Structural identification of production functions, Working paper, UCLA, Los Angeles.
- Amemiya, T. (1974), 'The nonlinear two-stage least-squares estimator', *Journal of Economic Literature* **2**, 105–110.
- Antràs, P. (2004), 'Is the U.S. aggregate production function Cobb-Douglas? New estimates of the elasticity of substitution', *Contributions to Macroeconomics* **4**(1).
- Atalay, E. (2014), 'Materials prices and productivity', *Journal of the European Economic Association* **12**(3), 575–611.
- Bentolila, S. & Saint-Paul, G. (2004), 'Explaining movements in the labor share', *Contributions to Macroeconomics* **3**(1).

- Binswanger, H. (1974), 'The measurement of technical change biases with many factors of production', *American Economic Review* **64**(6), 964–976.
- Black, S. & Lynch, L. (2001), 'How to compete: The impact of workplace practices and information technology on productivity', *Review of Economics and Statistics* **83**(3), 434–445.
- Blanchard, O. (1997), 'The medium run', *Brookings Papers on Economic Activity: Macroeconomics* **1997**(2), 89–158.
- Bloom, N., Sadun, R. & Van Reenen, J. (2012), 'Americans do IT better: US multinationals and the productivity miracle', *American Economic Review* **102**(1), 167–201.
- Brown, M. & de Cani, J. (1963), 'Technological change and the distribution of income', *International Economic Review* **4**(3), 289–309.
- Bruno, M. (1984), 'Raw materials, profits, and the productivity slowdown', *Quarterly Journal of Economics* **99**(1), 1–30.
- Buettner, T. (2005), R&D and the dynamics of productivity, Working paper, LSE, London.
- Caballero, R. & Hammour, M. (1998), 'Jobless growth: appropriability, factor substitution, and unemployment', *Carnegie-Rochester Conference Series on Public Policy* **48**, 51–94.
- Card, D. & DiNardo, J. (2002), 'Skill-biased technological change and rising wage inequality: Some problems and puzzles', *Journal of Labor Economics* **20**(4), 733–783.
- Caselli, F. (2005), Accounting for cross-country income differences, in P. Aghion & S. Durlauf, eds, 'Handbook of Economic Growth', Vol. 1A, North-Holland, Amsterdam, pp. 679–741.
- Chirinko, R. (2008), ' σ : The long and short of it', *Journal of Multivariate Analysis* **30**, 671–686.
- David, P. & van de Klundert, T. (1965), 'Biased efficiency growth and capital-labor substitution in the U.S., 1899-1960', *American Economic Review* **55**(3), 357–394.
- Davis, S. & Haltiwanger, J. (1992), 'Gross job creation, gross job destruction, and employment reallocation', *Quarterly Journal of Economics* **107**(3), 819–863.
- de La Grandville, O. (1989), 'In quest of the Slutsky diamond', *American Economic Review* **79**(3), 468–481.
- Dolado, J., Garcia-Serrano, C. & Jimeno, J. (2002), 'Drawing lessons from the boom of temporary jobs in Spain', *Economic Journal* **112**(480), 270–295.
- Doraszelski, U. & Jaumandreu, J. (2013), 'R&D and productivity: Estimating endogenous productivity', *Review of Economic Studies* **80**(4), 1338–1383.
- Dunne, T., Roberts, M. & Samuelson, L. (1988), 'Patterns of firm entry and exit in U.S. manufacturing', *Rand Journal of Economics* **19**(4), 495–515.
- Eslava, M., Haltiwanger, J., Kugler, A. & Kugler, M. (2004), 'The effects of structural reforms on productivity and profitability enhancing reallocation: Evidence from Colombia', *Journal of Development Economics* **75**, 333–371.

- European Commission (2001), ‘Statistics on innovation in Europe’, Enterprise DG, Brussels.
- European Commission (2004), ‘European competitiveness report’, Enterprise DG, Brussels.
- Foster, L., Haltiwanger, J. & Syverson, C. (2008), ‘Reallocation, firm turnover, and efficiency: Selection on productivity or profitability?’, *American Economic Review* **98**(1), 394–425.
- Foster, L., Haltiwanger, J. & Syverson, C. (2013), The slow growth of new plants: Learning about demand?, Working paper, University of Chicago, Chicago.
- Gandhi, A., Navarro, S. & Rivers, D. (2013), On the identification of production functions: How heterogeneous is productivity?, Working paper, University of Wisconsin.
- Gordon, R. (1990), *The measurement of durable goods prices*, National Bureau of Economic Research Monograph Series, University of Chicago Press, Chicago.
- Grieco, P., Li, S. & Zhang, H. (2015), ‘Production function estimation with unobserved input price dispersion’, *International Economic Review* **forthcoming**.
- Griliches, Z. (1998), *R&D and productivity: The econometric evidence*, University of Chicago Press, Chicago.
- Griliches, Z. (2000), *R&D, education, and productivity: A retrospective*, Harvard University Press, Cambridge.
- Griliches, Z. & Mairesse, J. (1998), Production functions: The search for identification, in S. Strom, ed., ‘Econometrics and Economic Theory in the 20th Century: The Ragnar Frisch Centennial Symposium’, Cambridge University Press, Cambridge.
- Grossman, G. & Helpman, E. (2002), ‘Integration versus outsourcing in industry equilibrium’, *Quarterly Journal of Economics* **117**(1), 85–120.
- Grossman, G. & Helpman, E. (2005), ‘Outsourcing in a global economy’, *Review of Economic Studies* **72**(1), 135–159.
- Hall, R. (1988), ‘The relation between price and marginal cost in U.S. industry’, *Journal of Political Economy* **96**(5), 921–947.
- Hammermesh, D. (1993), *Labor demand*, Princeton University Press, Princeton.
- Hammermesh, D. & Pfann, G. (1996), ‘Adjustment costs in factor demand’, *Journal of Economic Literature* **34**(3), 1264–1292.
- Hansen, L. (1982), ‘Large sample properties of generalized method of moments estimators’, *Econometrica* **50**(4), 1029–1054.
- Hicks, J. (1932), *The theory of wages*, Macmillan, London.
- Jin, H. & Jorgenson, D. (2010), ‘Econometric modeling of technical change’, *Journal of Econometrics* **157**(2), 205–219.
- Jones, C. (2005), ‘The shape of production functions and the direction of technical change’, *Quarterly Journal of Economics* **120**(2), 517–549.

- Jorgenson, D. (1995a), *Productivity. Volume 1: Postwar U.S. economic growth*, MIT Press, Cambridge.
- Jorgenson, D. (1995b), *Productivity. Volume 2: International comparisons of economic growth*, MIT Press, Cambridge.
- Judd, K. (1998), *Numerical methods in economics*, MIT Press, Cambridge.
- Kalt, J. (1978), ‘Technological change and factor substitution in the United States: 1929–1967’, *International Economic Review* **19**(3), 761–775.
- Klump, R. & de La Grandville, O. (2000), ‘Economic growth and the elasticity of substitution: Two theorems and some suggestions’, *American Economic Review* **90**(1), 282–291.
- Klump, R., McAdam, P. & Willman, A. (2007), ‘Factor substitution and factor-augmenting technical progress in the United States: A normalized supply-side system approach’, *Review of Economics and Statistics* **89**(1), 183–192.
- Krueger, A. (1999), ‘Measuring labor’s share’, *American Economic Review* **90**(2), 45–51.
- Kugler, M. & Verhoogen, E. (2012), ‘Prices, plant size, and product quality’, *Review of Economic Studies* **79**, 307–339.
- Levinsohn, J. & Petrin, A. (2003), ‘Estimating production functions using inputs to control for unobservables’, *Review of Economic Studies* **70**(2), 317–341.
- Lucas, R. (1969), Labor-capital substitution in U.S. manufacturing, in A. Harberger & M. Bailey, eds, ‘The taxation of income from capital’, Brookings Institution, Washington, pp. 223–274.
- Lucas, R. (1988), ‘On the mechanics of economic development’, *Journal of Monetary Economics* **22**(1), 3–42.
- Machin, S. & Van Reenen, J. (1998), ‘Technology and changes in skill structure: Evidence from seven OECD countries’, *Quarterly Journal of Economics* **113**(4), 1215–1244.
- Marschak, J. & Andrews, W. (1944), ‘Random simultaneous equations and the theory of production’, *Econometrica* **12**(3), 143–205.
- Marshall, A. (1920), *Principles of economics*, 8th edn, Macmillan, London.
- McAdam, P. & Willman, A. (2013), ‘Medium run redux’, *Macroeconomic Dynamics* **17**(4), 695–727.
- Newey, W., Powell, J. & Vella, F. (1999), ‘Nonparametric estimation of triangular simultaneous equations models’, *Econometrica* **67**(3), 565–603.
- Oberfeld, E. & Raval, D. (2014), Micro data and macro technology, Working paper, Federal Trade Commission, Washington.
- OECD (2007), ‘The policy mix for research, development and innovation in Spain: Key issues and policy recommendations’, Directorate for Science, Technology and Industry, Paris.

- Oi, W. & Idson, T. (1999), Firm size and wages, *in* O. Ashenfelter & D. Card, eds, ‘Handbook of labor economics’, Vol. 3, Elsevier, Amsterdam.
- Olley, S. & Pakes, A. (1996), ‘The dynamics of productivity in the telecommunications industry’, *Econometrica* **64**(6), 1263–1297.
- Raval, D. (2013), Non neutral technology differences, Working paper, Federal Trade Commission, Washington.
- Roberts, M. & Supina, D. (1996), ‘Output price, markups, and producer size’, *European Economic Review* **40**, 909–921.
- Robinson, P. (1988), ‘Root-n-consistent semiparametric regression’, *Econometrica* **56**(4), 931–954.
- Romer, P. (1990), ‘Endogenous technological change’, *Journal of Political Economy* **98**(5), S71–S102.
- Rotemberg, J. & Woodford, M. (1996), ‘Imperfect competition and the effects of energy price increases on economic activity’, *Journal of Money, Credit and Banking* **28**(4), 549–577.
- Solow, R. (1957), ‘Technical change and the aggregate production function’, *Review of Economics and Statistics* **39**(3), 312–320.
- Uzawa, H. (1961), ‘Neutral inventions and the stability of growth equilibrium’, *Review of Economic Studies* **28**(2), 117–124.
- Van Biesebroeck, J. (2003), ‘Productivity dynamics with technology choice: An application to automobile assembly’, *Review of Economic Studies* **70**, 167–198.
- Van Reenen, J. (1997), ‘Employment and technological innovation: Evidence from UK manufacturing firms’, *Journal of Labor Economics* **15**(2), 255–284.
- Violante, G. (2008), Skill-biased technical change, *in* S. Durlauf & L. Blume, eds, ‘The New Palgrave Dictionary of Economics’, 2nd edn, Palgrave Macmillan, New York.
- Wooldridge, J. (2004), On estimating firm-level production functions using proxy variables to control for unobservables, Working paper, Michigan State University, East Lansing.
- Wooldridge, J. (2010), *Econometric analysis of cross section and panel data*, 2nd edn, MIT Press, Cambridge.
- Zhang, H. (2014a), Biased technology and contribution of technological change to economic growth: Firm-level evidence, Working paper, University of Hong Kong, Hong Kong.
- Zhang, H. (2014b), Biased technology and productivity growth: Firm-level evidence from China’s steel industry, Slide deck, University of Hong Kong, Hong Kong.

Table 1: Descriptive statistics.

Industry	Obs. ^a	Firms ^a	Rates of growth ^b								
			Output (s. d.)	Capital (s. d.)	Labor (s. d.)	Materials (s. d.)	Price (s. d.)	$\frac{M}{L}$ (s. d.)	$\frac{P_M}{W}$ (s. d.)	$\frac{M}{K}$ (s. d.)	$\frac{P_M}{P_K}$ (s. d.)
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
1. Metals and metal products	2365	313	0.045 (0.235)	0.051 (0.192)	0.008 (0.161)	0.030 (0.327)	0.017 (0.052)	0.022 (0.316)	-0.008 (0.176)	-0.021 (0.373)	0.049 (0.099)
2. Non-metallic minerals	1270	163	0.046 (0.228)	0.057 (0.212)	0.010 (0.177)	0.041 (0.285)	0.012 (0.058)	0.031 (0.272)	-0.012 (0.147)	-0.016 (0.333)	0.043 (0.104)
3. Chemical products	2168	299	0.060 (0.228)	0.062 (0.182)	0.015 (0.170)	0.044 (0.274)	0.008 (0.055)	0.029 (0.250)	-0.015 (0.153)	-0.019 (0.313)	0.044 (0.141)
4. Agric. and ind. machinery	1411	178	0.031 (0.252)	0.040 (0.190)	-0.003 (0.169)	0.018 (0.347)	0.015 (0.026)	0.022 (0.335)	-0.015 (0.155)	-0.021 (0.390)	0.041 (0.099)
5. Electrical goods	1505	209	0.059 (0.268)	0.041 (0.173)	0.010 (0.205)	0.048 (0.359)	0.008 (0.046)	0.038 (0.344)	-0.021 (0.174)	0.007 (0.394)	0.045 (0.095)
6. Transport equipment	1206	161	0.060 (0.287)	0.043 (0.164)	0.004 (0.201)	0.051 (0.375)	0.008 (0.031)	0.047 (0.343)	-0.019 (0.171)	0.008 (0.396)	0.033 (0.093)
7. Food, drink and tobacco	2455	327	0.023 (0.206)	0.047 (0.177)	0.003 (0.169)	0.012 (0.286)	0.021 (0.054)	0.009 (0.295)	-0.018 (0.176)	-0.035 (0.328)	0.049 (0.116)
8. Textile, leather and shoes	2368	335	0.004 (0.229)	0.031 (0.189)	-0.015 (0.180)	-0.009 (0.348)	0.015 (0.042)	0.006 (0.355)	-0.021 (0.183)	-0.040 (0.385)	0.040 (0.099)
9. Timber and furniture	1445	207	0.025 (0.225)	0.045 (0.168)	0.013 (0.184)	0.014 (0.335)	0.020 (0.031)	0.001 (0.329)	-0.019 (0.171)	-0.031 (0.371)	0.067 (0.123)
10. Paper and printing products	1414	183	0.031 (0.187)	0.052 (0.221)	-0.001 (0.149)	0.013 (0.252)	0.017 (0.074)	0.014 (0.247)	-0.017 (0.159)	-0.039 (0.326)	0.046 (0.122)

^a Including $S_{Tjt} = L_{Tjt} = 0$.

^b Computed for 1991 to 2006.

Table 2: Descriptive statistics.

Industry	Intrafirm max-min												
	Temp. labor		Share			Hours		Outsourcing		With R&D			
	Obs. (%)	Share (s. d.)	Share of temp. (s. d.)	Hours worked ^a (s. d.)	Hours per worker ^a (s. d.)	Obs. (%)	Share (s. d.)	Obs. (%)	Share (s. d.)	Stable (%)	Occas. (%)	R&D (s. d.)	intens. (s. d.)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)				
1. Metal and metal products	1877 (79.4)	0.260 (0.221)	0.243 (0.197)	0.448 (0.360)	0.069 (0.090)	1014 (42.9)	0.200 (0.193)	56 (17.9)	109 (34.8)	0.012 (0.018)			
2. Non-metallic minerals	1018 (80.2)	0.231 (0.207)	0.232 (0.183)	0.482 (0.403)	0.065 (0.063)	316 (24.9)	0.177 (0.179)	20 (12.3)	62 (38.0)	0.011 (0.022)			
3. Chemical products	1722 (79.4)	0.170 (0.176)	0.203 (0.185)	0.446 (0.427)	0.043 (0.038)	924 (42.6)	0.146 (0.183)	121 (40.5)	85 (28.4)	0.026 (0.034)			
4. Agric. and ind. machinery	1069 (75.8)	0.189 (0.181)	0.227 (0.181)	0.485 (0.419)	0.086 (0.166)	808 (57.3)	0.288 (0.263)	64 (36.0)	62 (34.8)	0.022 (0.026)			
5. Electrical goods	1221 (81.1)	0.245 (0.206)	0.280 (0.216)	0.559 (0.452)	0.063 (0.077)	763 (50.7)	0.181 (0.194)	83 (39.7)	61 (29.2)	0.029 (0.040)			
6. Transport equipment	962 (79.8)	0.206 (0.198)	0.239 (0.184)	0.555 (0.415)	0.131 (0.237)	637 (52.8)	0.233 (0.261)	60 (37.3)	56 (34.8)	0.028 (0.049)			
7. Food, drink and tobacco	2067 (84.2)	0.276 (0.237)	0.266 (0.215)	0.468 (0.343)	0.058 (0.065)	514 (20.9)	0.142 (0.172)	65 (19.9)	86 (26.3)	0.007 (0.022)			
8. Textile, leather and shoes	1726 (79.2)	0.238 (0.260)	0.291 (0.244)	0.489 (0.402)	0.062 (0.086)	1214 (51.3)	0.252 (0.237)	44 (13.1)	85 (25.4)	0.017 (0.031)			
9. Timber and furniture	1175 (81.3)	0.320 (0.226)	0.326 (0.234)	0.523 (0.387)	0.056 (0.076)	535 (37.0)	0.183 (0.201)	21 (10.1)	44 (21.3)	0.010 (0.017)			
10. Paper and printing products	1024 (72.4)	0.155 (0.145)	0.221 (0.196)	0.425 (0.346)	0.057 (0.065)	679 (48.0)	0.273 (0.253)	17 (9.3)	48 (26.2)	0.015 (0.028)			

^a Computed as difference in logs.

Table 3: Elasticity of substitution.

Industry	Obs. ^a	Firms ^a	OLS		GMM incl. m_{jt-1} as instr.		GMM excl. m_{jt-1} as instr.			
			σ (s. e.)	δ_L (s. e.)	σ (s. e.)	χ^2 (df)	p val.	σ (s. e.)	χ^2 (df)	p val.
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
1. Metals and metal products	2365	313	1.163 (0.104)	0.023 (0.007)	0.451 (0.096)	57.846 (40)	0.034	0.694 (0.113)	13.683 (15)	0.550
2. Non-metallic minerals	1270	163	1.227 (0.119)	0.038 (0.008)	0.643 (0.086)	46.068 (40)	0.234	0.603 (0.126)	11.299 (15)	0.731
3. Chemical products	2168	299	1.132 (0.095)	0.016 (0.007)	0.481 (0.099)	65.068 (40)	0.007	0.618 (0.124)	7.582 (15)	0.939
4. Agric. and ind. machinery	1411	178	1.239 (0.166)	0.019 (0.008)	0.502 (0.114)	56.166 (40)	0.046	0.598 (0.103)	8.500 (15)	0.902
5. Electrical goods	1505	209	1.402 (0.163)	0.017 (0.009)	0.469 (0.108)	60.674 (40)	0.019	0.458 (0.108)	17.457 (15)	0.292
6. Transport equipment	1206	161	1.161 (0.218)	0.029 (0.011)	1.204 (0.089)	48.449 (40)	0.169	0.512 (0.162)	7.740 (15)	0.934
7. Food, drink and tobacco	2455	327	1.421 (0.094)	0.015 (0.008)	0.614 (0.063)	70.492 (40)	0.002	0.707 (0.084)	15.088 (15)	0.445
8. Textile, leather and shoes	2368	335	1.846 (0.169)	0.001 (0.100)	0.059 (0.077)	55.178 (40)	0.056	0.724 (0.162)	18.453 (15)	0.240
9. Timber and furniture	1445	207	0.793 (0.117)	0.014 (0.008)	0.461 (0.089)	37.357 (40)	0.590	0.486 (0.102)	5.805 (15)	0.983
10. Paper and printing products	1414	183	1.120 (0.107)	0.026 (0.008)	0.609 (0.057)	51.798 (40)	0.100	0.854 (0.077)	7.300 (15)	0.949

^a Including $S_{Tjt} = L_{Tjt} = 0$.

Table 4: Elasticity of substitution (cont'd).

Industry	Obs. ^a	Firms ^a	GMM		GMM with quality-corrected wage as instr.			
			σ (s. e.)	χ^2 (df)	p val.	σ (s. e.)	χ^2 (df)	p val.
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
1. Metals and metal products	1759	278	0.535 (0.114)	48.882 (38)	0.111	0.456 (0.112)	52.058 (38)	0.064
2. Non-metallic minerals	959	146	0.730 (0.098)	46.890 (38)	0.153	0.833 (0.096)	45.105 (38)	0.199
3. Chemical products	1610	269	0.696 (0.102)	46.154 (38)	0.171	0.695 (0.072)	48.889 (38)	0.111
4. Agric. and ind. machinery	979	164	0.607 (0.196)	42.420 (38)	0.286	0.762 (0.206)	44.227 (38)	0.225
5. Electrical goods	1147	191	0.592 (0.123)	46.782 (38)	0.155	0.624 (0.125)	44.592 (38)	0.214
6. Transport equipment	896	146	0.798 (0.088)	45.740 (38)	0.182	0.602 (0.097)	41.214 (38)	0.332
7. Food, drink and tobacco	1963	306	0.616 (0.081)	53.931 (38)	0.045	0.766 (0.079)	38.379 (38)	0.452
8. Textile, leather and shoes	1593	282	0.440 (0.186)	52.496 (38)	0.059	0.462 (0.149)	55.996 (38)	0.030
9. Timber and furniture	1114	188	0.438 (0.093)	39.204 (38)	0.416	0.497 (0.094)	36.687 (38)	0.530
10. Paper and printing products	938	162	0.525 (0.088)	44.508 (38)	0.217	0.449 (0.085)	43.009 (38)	0.265

^a Excluding $S_{Tjt} = L_{Tjt} = 0$.

Table 5: Labor-augmenting technological change.

Industry	$\Delta\omega_L$ (1)	$corr(\Delta\omega_L, \omega_L)$ (2)	$\frac{\omega_L}{R\&D-No\ R\&D}$ (4)	$\frac{\epsilon_L \Delta\omega_L}{R\&D-No\ R\&D}$ (3)	$\frac{\epsilon_L \Delta\omega_L}{R\&D-No\ R\&D}$ (5)	$\frac{\epsilon_L \Delta\omega_L}{No\ R\&D}$ (6)	Skill upgrading			
							σ (s. e.) (7)	$\chi^2 (df)$ (8)	p val. (9)	$\Delta\omega_L$ (10)
1. Metals and metal products	0.091	0.183	0.885	0.021	0.024	0.018	0.582 (0.117)	44.868 (38)	0.206	0.104
2. Non-metallic minerals	0.142	0.191	1.461	0.031	0.022	0.028	0.737 (0.092)	35.898 (38)	0.567	0.087
3. Chemical products	0.049	0.186	1.239	0.013	0.018	-0.002	0.618 (0.110)	47.832 (38)	0.132	0.053
4. Agric. and ind. machinery	0.126	0.209	1.537	0.032	0.028	0.046	0.177 (0.172)	38.413 (38)	0.451	0.060
5. Electrical goods	0.220	0.237	2.783	0.022	0.022	0.012	0.488 (0.129)	48.365 (38)	0.121	0.179
6. Transport equipment	0.183	0.261	0.637	0.036	0.045	0.012	0.781 (0.101)	45.457 (38)	0.189	0.098
7. Food, drink and tobacco	0.018	0.131	-0.044	0.007	0.009	0.006	0.655 (0.084)	53.981 (38)	0.045	-0.007
8. Textile, leather and shoes	0.010	0.179	0.480	0.007	0.007	0.009	0.120 (0.168)	41.931 (38)	0.304	0.000
9. Timber and furniture	-0.013	0.142	-0.024	0.002	0.007	0.002	0.528 (0.090)	37.674 (38)	0.484	-0.023
10. Paper and printing products	0.021	0.094	0.579	0.014	0.007	0.020	0.396 (0.082)	37.418 (38)	0.496	-0.011

Table 6: Distributional parameters and elasticity of scale.

Industry	GMM			
	β_K	ν	$\chi^2(df)$	p val.
	(s. e.)	(s. e.)		
	(1)	(2)	(3)	(4)
1. Metals and metal products	0.232 (0.073)	0.941 (0.029)	2.872 (8)	0.942
2. Non-metallic minerals	0.225 (0.133)	0.911 (0.063)	3.975 (8)	0.859
3. Chemical products	0.136 (0.059)	0.934 (0.041)	1.074 (8)	0.998
4. Agric. and ind. machinery	0.139 (0.125)	0.806 (0.088)	7.258 (9)	0.610
5. Electrical goods	0.133 (0.038)	0.848 (0.046)	3.059 (10)	0.980
6. Transport equipment ^a	0.308 (0.182)	0.923 (0.061)		
7. Food, drink and tobacco	0.303 (0.137)	0.931 (0.040)	2.006 (8)	0.981
8. Textile, leather and shoes	0.066 (0.097)	0.976 (0.035)	3.269 (9)	0.953
9. Timber and furniture	0.103 (0.107)	0.932 (0.066)	9.748 (8)	0.283
10. Paper and printing products	0.227 (0.080)	0.936 (0.036)	5.402 (8)	0.714

^a We have been unable to compute the second-step GMM estimate.

Table 7: Hicks-neutral technological change.

Industry	$\Delta\omega_H$ (1)	$corr(\Delta\omega_H, \omega_H)$ (2)	$\epsilon_L \Delta\omega_L + \Delta\omega_H$ (3)	$corr(\Delta\omega_H, \Delta\omega_L)$ (4)	Firms' R&D activities		
					ω_H		$\Delta\omega_H$
					R&D-No R&D (5)	R&D (6)	
1. Metals and metal products	0.044	0.346	0.065	0.686	0.027	0.046	0.038
2. Non-metallic minerals	0.005	0.448	0.036	0.439	0.078	-0.019	0.041
3. Chemical products	0.019	0.220	0.032	0.717	0.182	0.022	0.011
4. Agric. and ind. machinery	0.041	0.264	0.072	0.678	0.382	0.039	0.022
5. Electrical goods	0.020	0.294	0.042	0.622	0.484	0.009	0.055
6. Transport equipment	0.042	0.714	0.078	0.549	0.121	0.058	-0.031
7. Food, drink and tobacco	0.001	0.214	0.007	0.817	-0.148	0.007	0.000
8. Textile, leather and shoes	0.012	0.295	0.019	0.612	-0.146	-0.003	0.032
9. Timber and furniture	0.021 ^a	0.323	0.023 ^a	0.714	-0.132	0.008	0.035
10. Paper and printing products	0.002	0.220	0.016	0.851	-0.104	0.007	0.006

^a We trim values of $\Delta\omega_H$ below -0.25 and above 0.5 . This amounts to trimming around one third of observations.

Table 8: Capital-augmenting technological change.

Industry	GMM						
	$\Delta\omega_K$ (1)	$\epsilon_K\Delta\omega_K$ (2)	β_K (s. e.) (3)	ν (s. e.) (4)	δ_K (s. e.) (5)	χ^2 (df) (6)	p val. (7)
1. Metals and metal products	0.056	0.004	0.254 (0.129)	0.903 (0.055)	0.036 (0.061)	2.947 (7)	0.890
2. Non-metallic minerals	-0.010	0.007	0.236 (0.102)	0.906 (0.072)	0.010 (0.072)	2.921 (7)	0.822
3. Chemical products	-0.018	0.001	0.125 (0.068)	0.942 (0.041)	-0.031 (0.092)	0.692 (7)	0.998
4. Agric. and ind. machinery	-0.020	0.000	0.182 (0.177)	0.801 (0.081)	0.031 (0.122)	8.148 (8)	0.419
5. Electrical goods	-0.078	0.000	0.129 (0.041)	0.845 (0.054)	-0.004 (0.056)	2.969 (9)	0.966
6. Transport equipment ^a	0.008	0.005	0.115 (0.088)	0.981 (0.050)	-0.143 (0.138)		
7. Food, drink and tobacco	-0.005	0.002	0.282 (0.286)	0.918 (0.058)	-0.045 (0.204)	2.378 (7)	0.936
8. Textile, leather and shoes ^a	-0.085	-0.002	0.080 (0.143)	0.971 (0.047)	0.053 (0.135)		
9. Timber and furniture	-0.042	0.000	0.088 (0.119)	0.924 (0.067)	-0.021 (0.059)	8.861 (7)	0.263
10. Paper and printing products	0.022	0.007	0.229 (0.089)	0.935 (0.033)	0.005 (0.045)	5.149 (7)	0.642

^a We have been unable to compute the second-step GMM estimate.

Table A1: Industry definitions and equivalent classifications.

Industry	Classifications		Share of value added	Number of subindustries	
	ESSE (1)	National Accounts (2)			ISIC (Rev. 4) (3)
1. Ferrous and non-ferrous metals and metal products	12+13	DJ	C 24+25	13.2	11
2. Non-metallic minerals	11	DI	C 23	8.2	8
3. Chemical products	9+10	DG-DH	C 20+21+22	13.9	7
4. Agricultural and industrial machinery	14	DK	C 28	7.1	7
5. Electrical goods	15+16	DL	C 26+27	7.5	13
6. Transport equipment	17+18	DM	C 29+30	11.6	7
7. Food, drink and tobacco	1+2+3	DA	C 10+11+12	14.5	10
8. Textile, leather and shoes	4+5	DB-DC	C 13+14+15	7.6	11
9. Timber and furniture	6+19	DD-DN 38	C 16+31	7.0	6
10. Paper and printing products	7+8	DE	C 17+18	8.9	4
Total				99.5	84

Table A2: Variation in the wage and its determinants.

Industry	Wage			Wage regression							
	CV	Var	Within (%)	Betw. (%)	Temp. (s. e.)	White (s. e.)	Engin. (s. e.)	Tech. (s. e.)	R^2	R^2_Q	R^2_C
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
1. Metals and metal products	0.425	39.025	9.779 (25.1)	29.246 (74.9)	-0.425 (0.057)	0.127 (0.097)	1.106 (0.298)	0.316 (0.094)	0.651	0.094	0.480
2. Non-metallic minerals	0.441	36.252	10.072 (27.8)	26.180 (72.2)	-0.098 (0.065)	0.124 (0.159)	0.896 (0.280)	0.246 (0.181)	0.742	0.020	0.643
3. Chemical products	0.440	54.332	9.673 (17.8)	44.659 (82.2)	-0.465 (0.066)	0.461 (0.074)	0.592 (0.137)	0.203 (0.099)	0.755	0.197	0.376
4. Agric. and ind. machinery	0.354	30.980	11.472 (37.0)	19.508 (63.0)	-0.273 (0.067)	0.285 (0.105)	0.803 (0.226)	-0.028 (0.125)	0.631	0.082	0.484
5. Electrical goods	0.383	31.047	8.461 (27.3)	22.586 (72.7)	-0.374 (0.058)	0.219 (0.073)	1.092 (0.264)	0.312 (0.087)	0.661	0.200	0.356
6. Transport equipment	0.393	40.666	12.876 (31.7)	27.790 (68.3)	-0.377 (0.079)	0.220 (0.108)	0.402 (0.300)	0.274 (0.166)	0.709	0.066	0.552
7. Food, drink and tobacco	0.502	36.590	5.952 (16.3)	30.638 (83.7)	-0.451 (0.053)	0.115 (0.053)	1.292 (0.265)	0.357 (0.154)	0.753	0.097	0.481
8. Textile, leather and shoes	0.449	16.565	3.654 (22.1)	12.911 (77.9)	-0.260 (0.048)	0.646 (0.084)	1.584 (0.402)	0.346 (0.241)	0.683	0.140	0.389
9. Timber and furniture	0.392	14.646	3.643 (24.9)	11.003 (75.1)	-0.356 (0.051)	0.173 (0.089)	0.288 (0.377)	0.002 (0.164)	0.697	0.061	0.525
10. Paper and printing products	0.464	51.667	10.003 (19.4)	41.664 (80.6)	-0.477 (0.099)	0.188 (0.084)	0.444 (0.210)	0.277 (0.127)	0.702	0.070	0.505